



THE FIELDS INSTITUTE FOR RESEARCH IN MATHEMATICAL SCIENCES

POSTDOCTORAL/GRADUATE STUDENT  
SEMINAR SERIES ON L-FUNCTIONS

SPEAKER:

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The Fields Institute

On the Topic:

The Average Value of L-Functions at the Critical Point

For a discriminant  $D$  of a binary quadratic form, we study the average value of  $L(s, \varepsilon_D)$  at the critical point  $\frac{1}{2}$  where  $\varepsilon_D$  is defined by W. Kohnen and D. Zagier :  $\varepsilon_D(n) = \sum_{\substack{g>0 \\ g|6, g^2|n \\ (6/g, n/g^2)=1}} (\frac{D_0}{g^{-2}n})g$  for  $n \in \mathbb{N}$  and  $D = D_0\delta^2$ ,  $D_0$  a fundamental discriminant and  $\delta \in \mathbb{N}$ . When  $D = D_0$ ,  $L(s, \varepsilon_{D_0})$  is the Dirichlet series  $L(s, (\frac{D_0}{\cdot}))$ . We derive an asymptotic formula for  $\sum_D L(\frac{1}{2}, \varepsilon_D)$ , where the sum runs over all discriminants  $D \in (0, Y]$  or  $[-Y, 0)$ .

Wednesday, September 29, 1993

1:30 pm, Room 3018

at

The Fields Institute