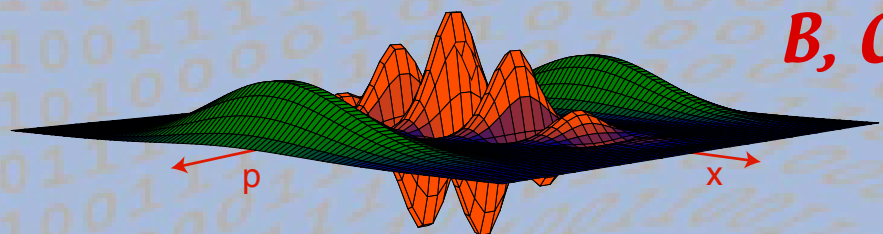
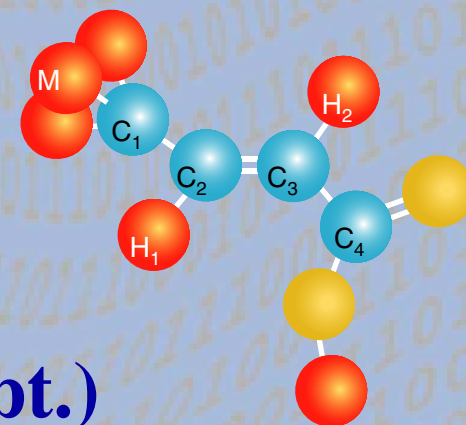


# NMR Quantum Information Processing



*B, CCS, T Divisions*



**Raymond Laflamme**  
(in U of Waterloo from Sept.)

<http://qso.lanl.gov/qc>

E. Knill, R. Martinez, W.H. Zurek,  
D. Cory (MIT),

C. Negrevergene (LANL), M. Nielsen (Caltech), L. Viola (LANL)



# ***QIP NMR experiments***

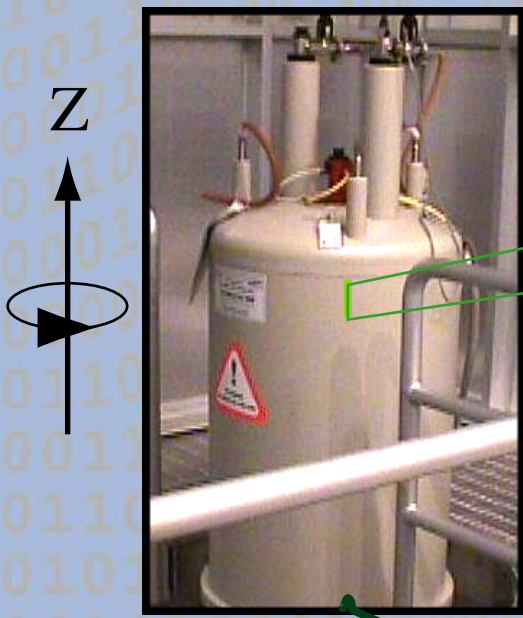
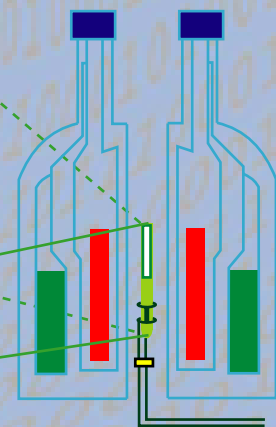
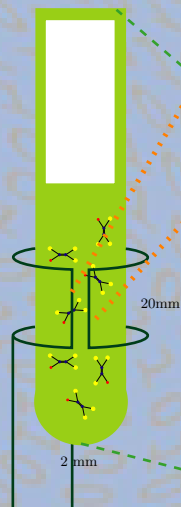
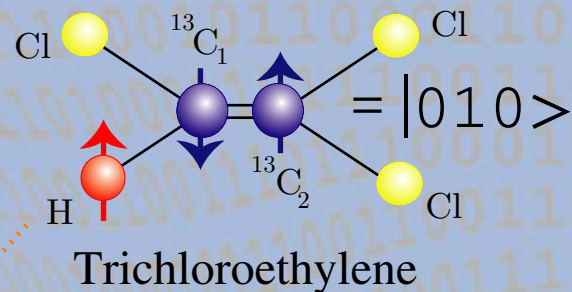
# of qubits	Algorithms	Year	Reference
2	Gates	1996	MIT, Stanford, NC, Oxford
	Database Search	1998	Oxford, IBM
	Deutsch-Josza	1998	Oxford, IBM
	Quantum Simulation	1999	MIT/LANL
	Quantum Fourier Transform	1998	MIT, CAS
	Dense Coding	1998	CAS
	Quantum Detecting Code	1999	IBM
3	GHZ state	1997	LANL, MIT
	Quantum Error Correction	1997	MIT/LANL
	Quantum Teleportation	1997	LANL
	Deutsch-Josza	1998	KAIST, India
	Quantum Simulation	1999	MIT/LANL
	Quantum Fourier Transform	1998	MIT
	Quantum Eraser	1998	MIT
4	$C^3$ -not Gate	1999	MIT
5	Deutsch-Josza	1999	Frankfurt
	Order finding	2000	IBM
6	Quantum Error Correction	2001	LANL
	Decoupling	1998	Cambridge
7	Benchmark	2000	LANL

# Liquid State NMR

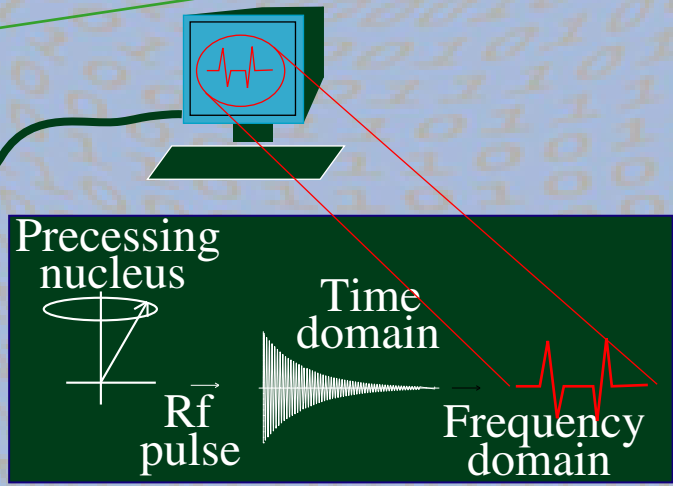
Cory & Havel PNAS, 64, 1634, 1997

Gershenfeld & Chuang, Science 275, 350, 1997

- Larmor Frequency ~ 500MHz
- Single bit gate: 1/ ~ms
- Two qubit gate: ~ 10ms
- $z^1 z^2$  interaction
- $T_2 \sim 1s$
- $T_1 \sim 5-30s$
- $\gamma = \gamma_1 - \gamma_2$

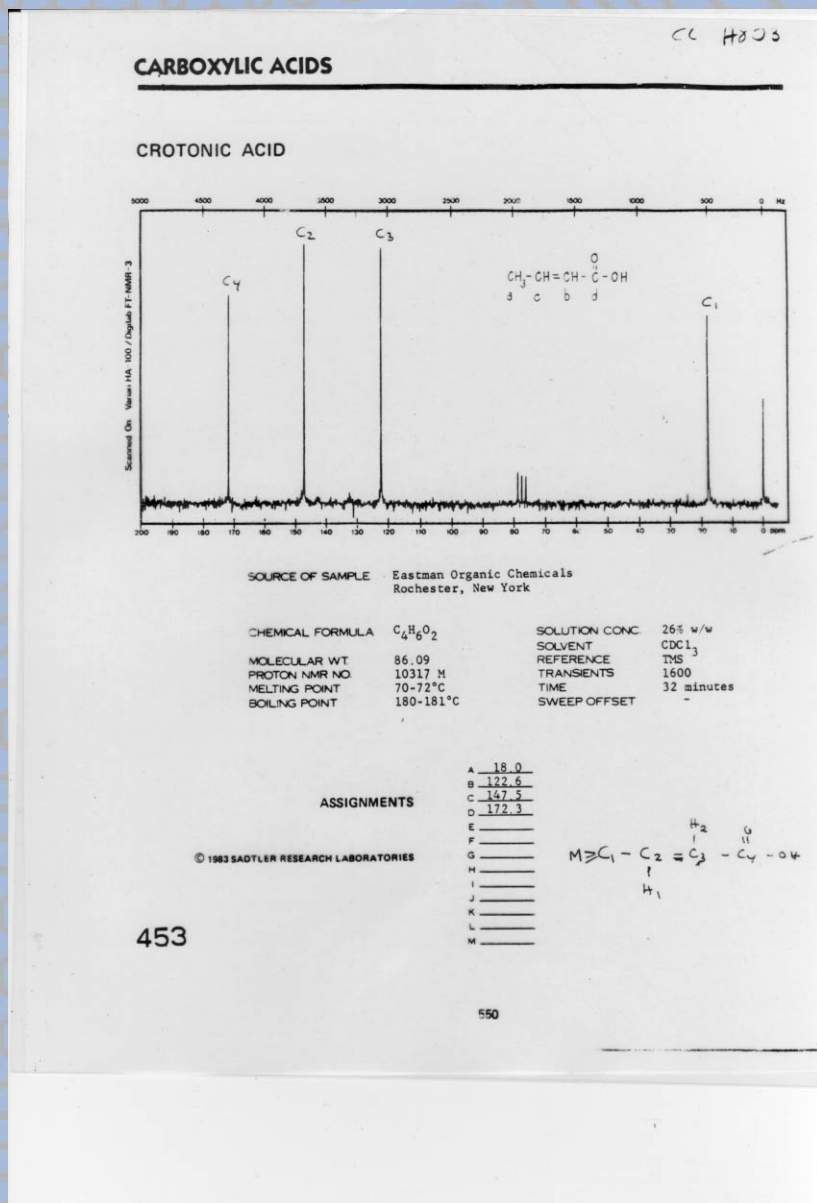


Bruker DRX-500



# Choosing a molecule

- ✳ different chemical shifts
- ✳ large decoherence times
- ✳ strong couplings



Rudy Martinez, B-2

Stable Isotope Laboratory  
at Los Alamos

	M	H <sub>1</sub>	H <sub>2</sub>	C <sub>1</sub>	C <sub>2</sub>	C <sub>3</sub>	C <sub>4</sub>
M	-969.4						
H <sub>1</sub>	6.9	-3560.3					
H <sub>2</sub>	-1.7	15.5	-2938.2				
C <sub>1</sub>	127.5	3.8	6.2	-2327.0			
C <sub>2</sub>	-7.1	156.0	-0.7	41.6	-18599.2		
C <sub>3</sub>	6.6	-1.8	162.9	1.6	69.7	-15412.8	
C <sub>4</sub>	-0.9	6.5	3.3	7.1	1.4	72.4	-21685.1

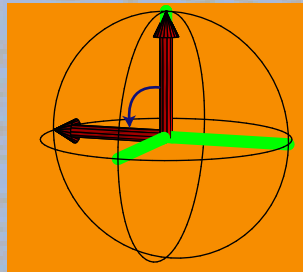
# Quantum Gates in NMR

## ☀ 1 bit gates

Rotation around x/y axis: e.g. around x

Rotation around z axis:

hard pulse: 10 μs;  
soft pulse 1/



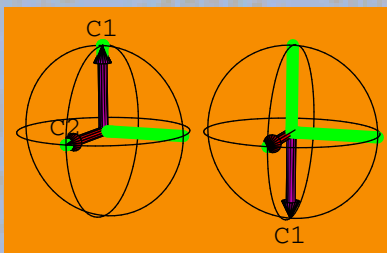
$$e^{i\mu X} = \mathbb{1} \cos \mu + iX \sin \mu$$

$$Z \rightarrow Z \cos \mu + Y \sin \mu$$

$$Y \rightarrow Y \cos \mu + Z \sin \mu$$

## ☀ 2 bit gates

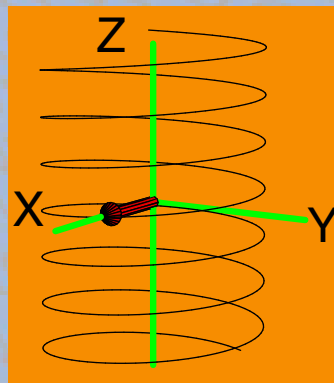
J coupling ~ 100 Hz



$$e^{iZZ} = \mathbb{1} \cos \mu + iZZ \sin \mu$$

$$X \rightarrow X \cos \mu + YZ \sin \mu$$

## ☀ Gradient field



$$I_+ = X + iY \quad e^{i\pi z} I_+$$

# State Preparation

$$\Omega = \frac{1}{2^n} e^{-H}$$

## \* Computational cooling

(DiVincenzo/ Knill/ Schulman & Vazirani: quant-ph9804060)

## \* Pseudo pure states

Havel & Cory 1996

Gershenfeld & Chuang 1996

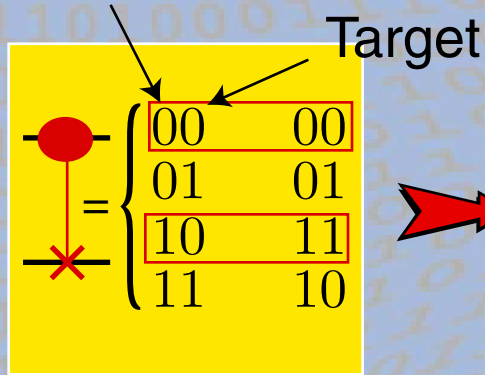
$$\Omega = \frac{1}{2^n} (I + H)$$

## \* 1 Pseudo pure qubit

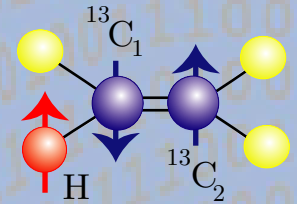
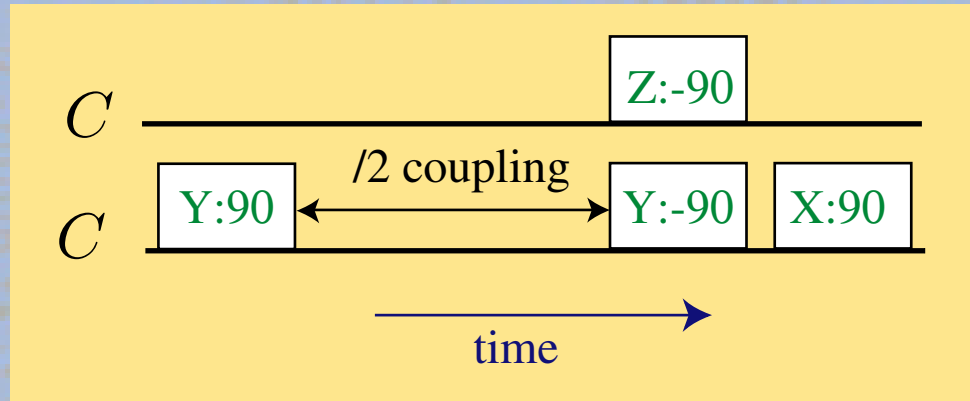
Knill & Laflamme, PRL 81, 5672, 1998

# From quantum algorithms to machine language

## Control-Not



## Quantum circuit



## Pre-compiler (Optimizer)

```
;; Debug to track down error sources by doing partial error correction.
#define Clobs
; !$watch{H1} = 1;
; !$watch{H2} = 1;
#include "clpp.h"

;> $locRng = 5; $locStp = 2;

; erate .1
;<
;> $locRng = 5; $locStp = 2;

; pulse noop FM:Z--
; Correction steps
;
; ;crot C1->C2
; pulse C2_90 .25
; zz .25 C1 C2
; zpulse C1:.75;C2:
; pulse C2_90 .75
; pulse C2_90 .0
; refocus C1C2_180
; delay end 0
;<
#include "crot_def
```

## Bruker (machine) language

```
1 ze
2 lhold LOCKH_OFF

d1
1u reset:f1
1u reset:f2
1m

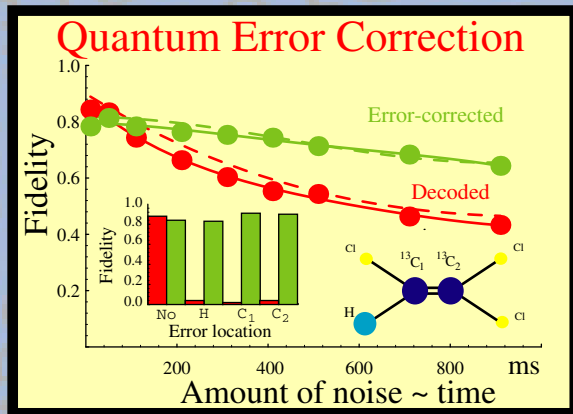
lhold LOCKH_ON

;Initial virtual 180
;Time: 0.000e+00 sec (C2_90:sp9 ph13 ):f1
8u
3u
(C2_90:sp9 ph13 ):f1
3u ipp13
3u ipp13
0.71365m
8u
8u
(C2_90:sp9 ph13 ):f1
6u ipp15 ipp13
8u
(C2_90:sp9 ph13 ):f1
6u ipp15 ipp13
3u fq1:f2
3u fq2:f1
go=2 ph0:r
100m
lhold LOCKH_OFF
8u
(C2_90:sp9 ph19):f1
6u ipp15 ipp19
8u
(C2_90:sp9 ph20):f1
6u ipp15 ipp20
```

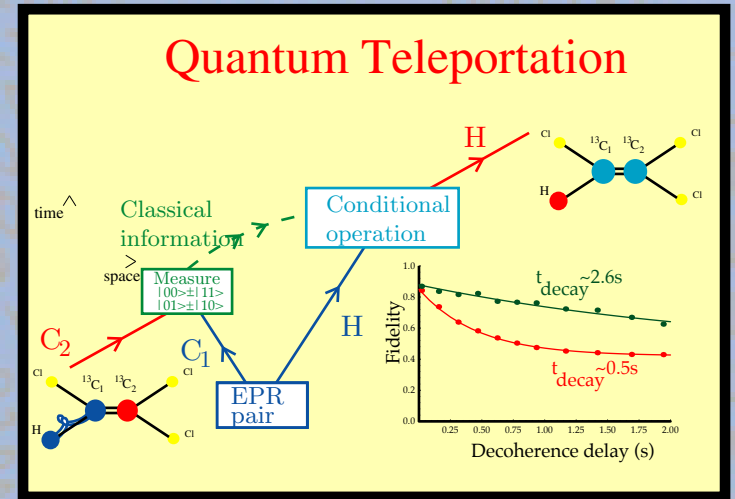
# Experiments

NMR-GHZ, R.L., E. Knill, W.H. Zurek,  
P. Catasti, S. Vellupillai,  
Proc.Roy.SocA356, 1941, 1998.

with MIT



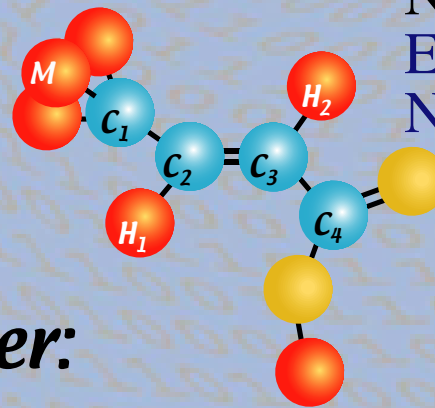
Science  
Top 10 breakthroughs  
of the year;  
Science 282,  
2156, 1998



Experimental Quantum Error  
Correction: D. G. Cory,  
M. D. Price, W. Maas, E. Knill,  
R. Laflamme, W. H. Zurek,  
T. F. Havel and S. S. Somaroo.  
PRL 81, 2152, 1998

Complete quantum  
teleportation using  
NMR: M. Nielsen,  
E. Knill, R. Laflamme  
Nature 396, 52, 1998

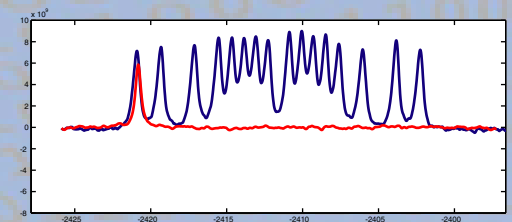
nature



nature

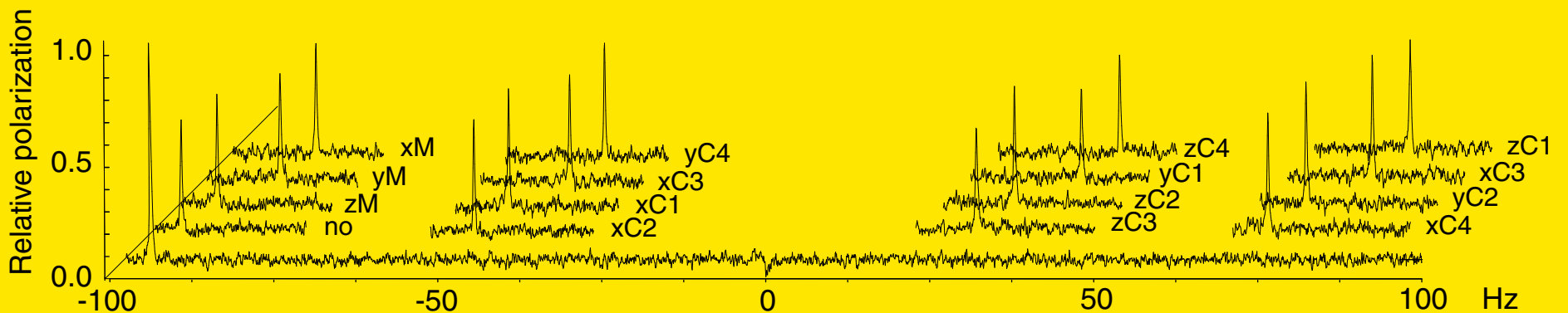
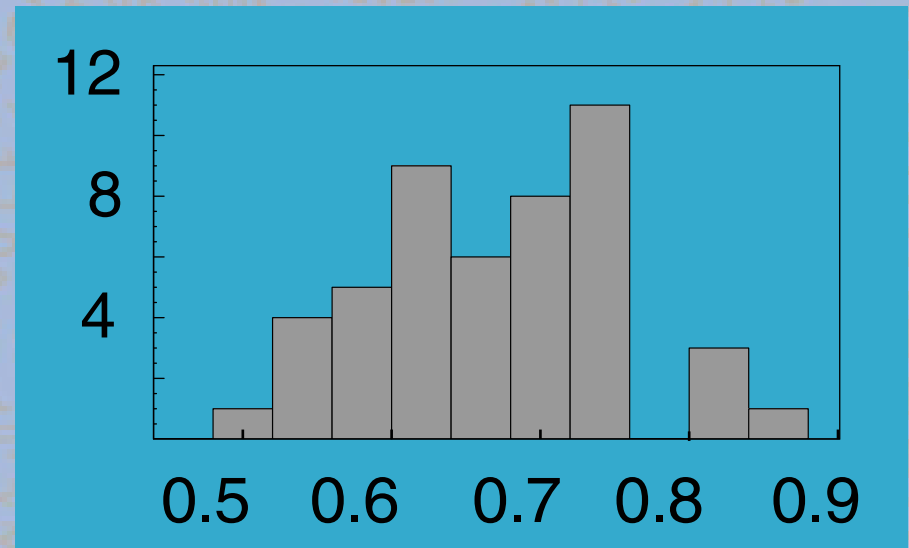
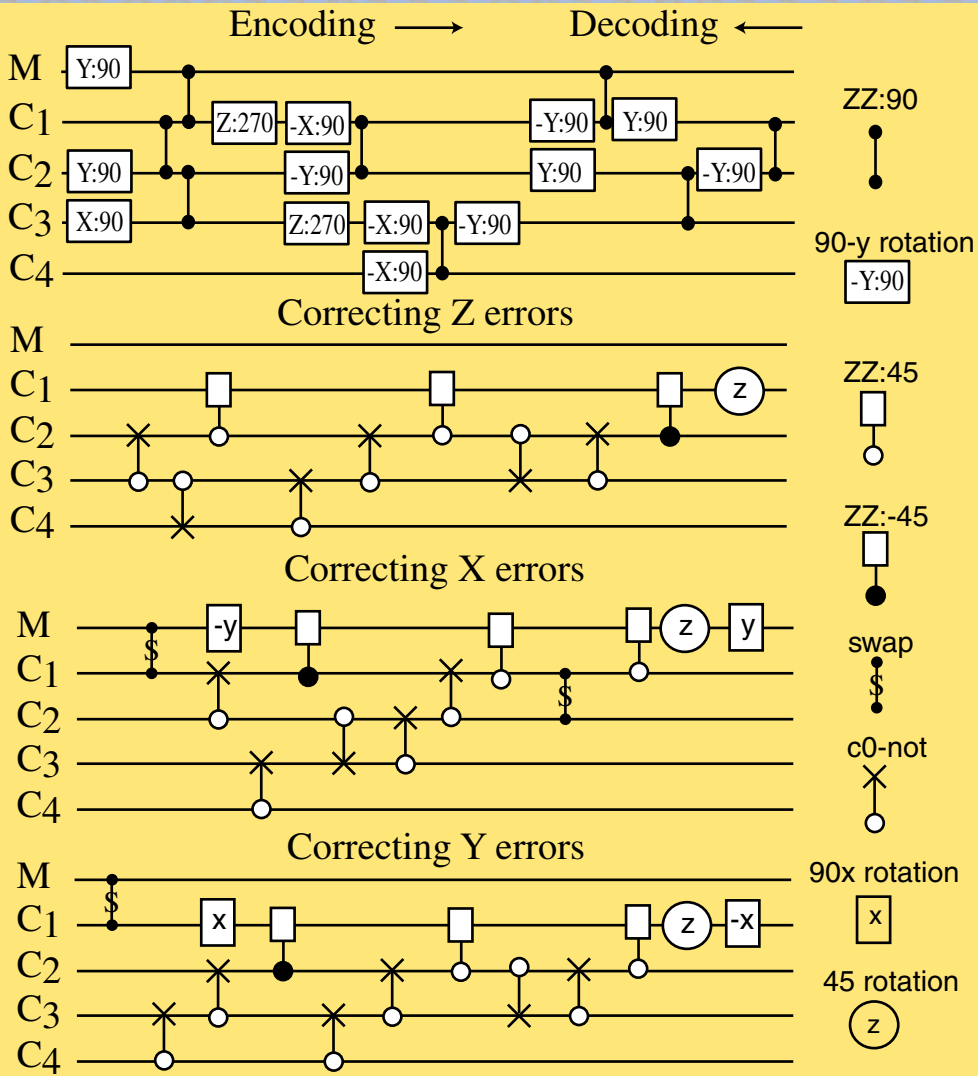
**A 7 bit quantum computer:**

An algorithmic benchmark for quantum information processing,  
E. Knill, R. L., R. Martinez, C.-H. Tseng, Nature 404, 368-370, 2000





# The perfect 5 bit quantum error correcting code



# Conclusion



“Many of today’s practical technologies result from basic science done years to decades before. The people involved, motivated mainly by curiosity; often have little idea as to where their research will lead. Our ability to forecast the practical payoffs from fundamental exploration of the nature of things (and, similarly, to know which of today’s research avenues are technological dead ends) is poor. This springs from a simple truth: new ideas discovered in the process of research are really new.”

Charles Townes  
in *How the Laser Happened*.

