

INET Workshop

# Mathematics for New Economic Thinking

Fields Institute for Research in Mathematical Sciences

31 October 2013

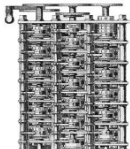
## The True Cost of OTC Derivatives

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[www.cfr.statslab.cam.ac.uk](http://www.cfr.statslab.cam.ac.uk)



Commenting in 1998 on the proposed repeal of the 1933 **Glass-Steagall Act** *separating commercial and investment banking* “ **an archaic set of restrictions**”

**Lawrence Summers**

US Secretary of the Treasury & Future President, Harvard University & Advisor, Citigroup

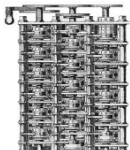
*Bloomberg Business Week*, 12<sup>th</sup> August 2013

“Commentators speak loosely about going back to **Glass-Steagall**. But the Glass-Steagall Act was **introduced to deal with a problem that no longer exists: the distribution of fraudulent securities to uniformed customers**”

**Martin Jacomb**

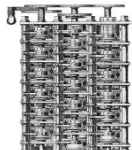
Chairman, Share PLC & Former Chancellor, Buckingham University

*Financial Times*, 14<sup>th</sup> September 2011



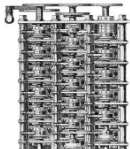


It is indeed the truth; one can do more fascinating things with an option than an inventive boy can do with a set of Meccano *New Yorker* (1937)



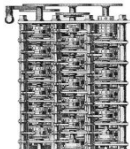
# Outline

- **Financial Market Developments**
- **Rôle of Structured OTC Derivatives**
- **Cost of OTC Derivatives to Clients**
- **Pricing Methodology**
- **Evolving Regulation of OTC Derivatives**



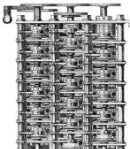
# Financial Market Developments 1980-2007

- **Technical changes** (market data, pricing calculations, spreadsheets, global communications, state-of-the-art computing hardware)
- **Regulatory changes** (Basel I and II )
- **Changing product paradigms** (risk transfer, transferring property, exchanging contractual obligations) leading to exponential growth of **over-the-counter** (OTC) **structured products**



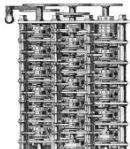
# Financial Services Trading Background 1980-2007

- From customer benefit to **shareholder benefit**
- Profits in **complexity of structured products**
- **Risk management** and **hedge portfolios**
- Risk-adjusted return on capital (**RAROC**)
- Ever **increasing leverage** due to global **tax regulation**
- Using **counterparty assets to preserve banks' regulatory capital**



# Power of OTC Structured Products for Clients

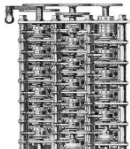
- Optimising **interest rate** and **FX liabilities** – **options** and **swaps**
- Hedging **default risk** - **credit default swaps** (CDSs) and **collateralized debt obligations** (CDOs)
- Profiting from **tax arbitrage** – **cross-border leasing** agreements



# Financial Crises 1980-2013

## ▪ Caused by

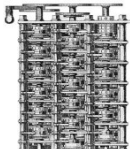
- **Inflation**
  - Russian default August 1998
- **Currency crashes**
  - Mexican peso crisis 1995. After NAFTA (Canada, Mexico, US)
- **Currency debasement**
  - Argentine default 2001. Failed US\$ peg with horrifying domestic consequences
- **Asset price bubbles**
  - South American debt crisis in the 1980s. Recycling 'petrodollars' in the 1970s
  - Black Monday October 1987. US credit expansion by Savings & Loans sector
  - Japanese crisis 1990. Property bubble fuelled by export led growth
  - Asian crisis 1997. Corporate debt burden financed by property bubbles & "hot" money
  - Internet bubble 2000. Irrational exuberance ?
  - US subprime crisis 2008. (Self) deception
  - Euro crisis 2010. Reality avoidance
  - China crisis 201?. Credit expansion to fuel export led growth





# This Time It's Different

- Financial crises have marked the development of capitalism since the Renaissance
- These have historically been connected with sovereign credit over the past 800 years [Reinhart & Rogoff \(2010\)](#)
- In his famous book [Kindleberger \(1989\)](#) gives a detailed account of financial crises in Europe and North America from 1618

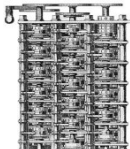


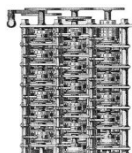
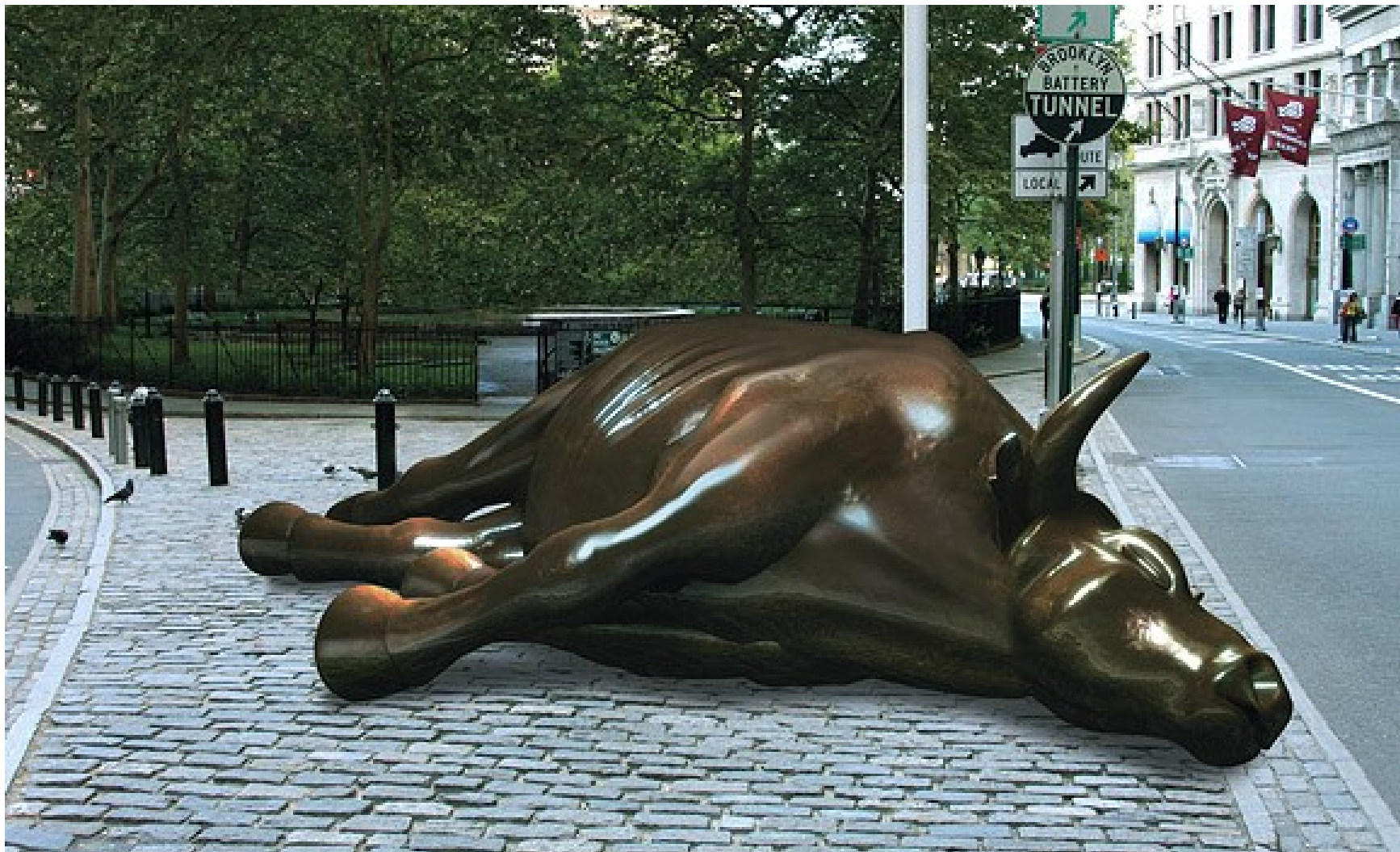
We have nothing to fear but fear itself

32<sup>nd</sup> President of the United States March 1933

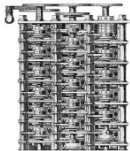
This sucker could go down

43<sup>rd</sup> President of the United States September 2008



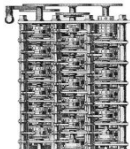


# 3. Rôle of Structured OTC Derivatives



# Views on the Rôle of Derivatives

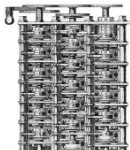
- **Guns don't kill people. People kill people!** **US National Rifle Association**
- **Derivatives are weapons of mass destruction** **Warren Buffet**
- **There are two types of derivatives – “bought” and “sold”**  
– in proportion 30% to **70%** **City MD**
- **Banking is the last industry to go “high tech” after aerospace, oil, manufacturing, airlines, logistics, film making, etc.**



# Generic Rate Swap Structure

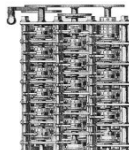


- Counterparty **A** converts from **fixed** to **floating**
- Counterparty **B** converts from **floating** to **fixed**
- Through an **over the counter** (OTC) product of a **swap dealer** who charges both parties a **spread**



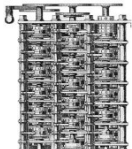
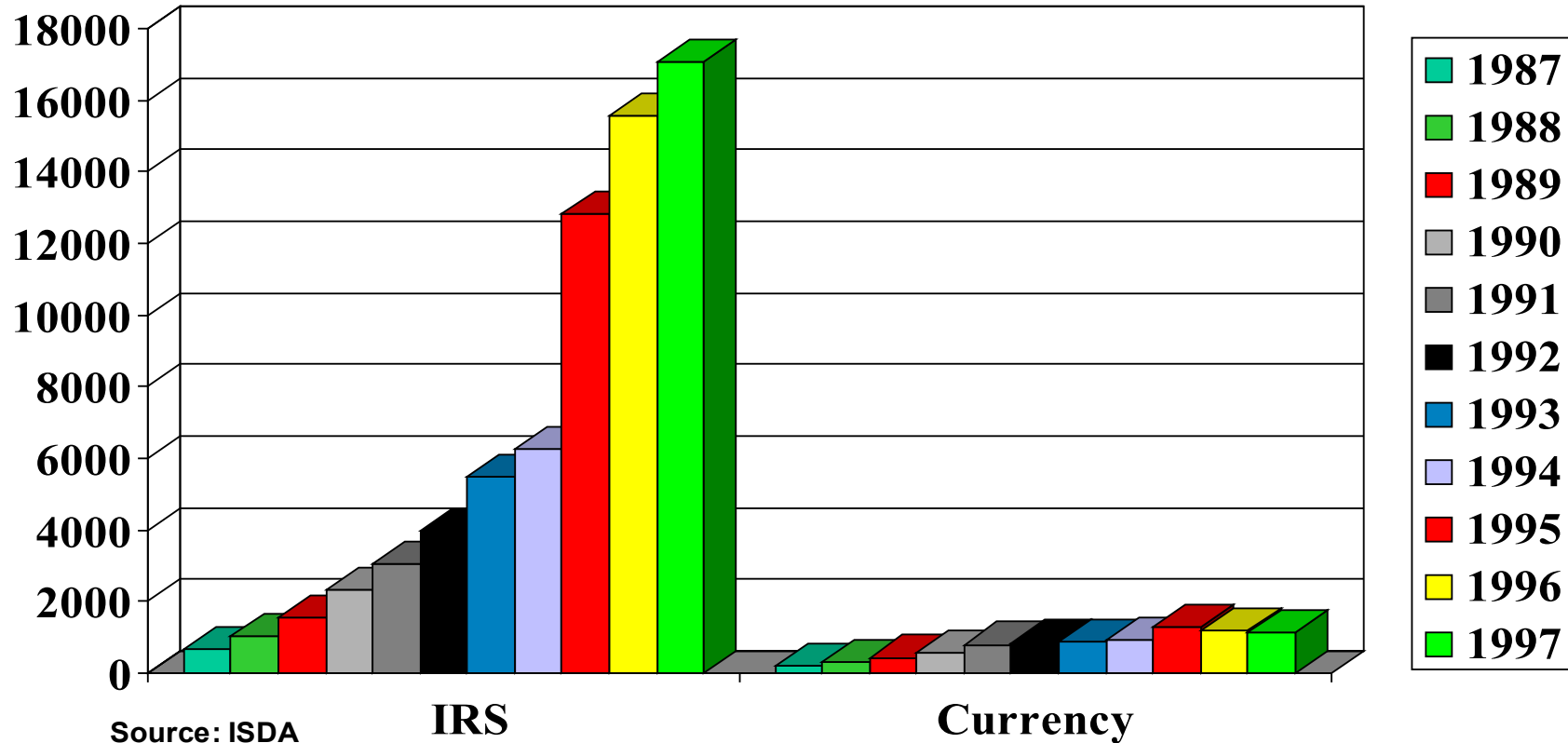
# Evolution of the Swap Market

- Began in the early 1970's
  - Collapse of Bretton Woods: floating currency rates and FX volatility
  - UK exchange controls
  - Parallel/back-to-back loans
  - IBM-World Bank swap of 1981
  
- Regulation & standardization
  - International Swap Dealers Association (ISDA) formed in 1985
    - Development of **Master Swap Agreement led to market takeoff**
  - Capital Adequacy
    - Basle Accord (1987), Federal Reserve Guidelines (1989)
  - Risk Measurement: VaR G30 (1993)



# First Decade Market Growth

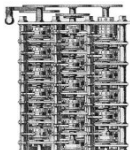
Market volume by end **1997** about **\$17 trillion** in notional principal  
and about **\$560 trillion now**





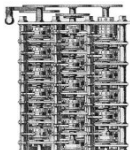
# Current State of Derivatives Dealing

- Structured **fixed income** and **credit derivative instruments** over the past two decades have enormously increased in value ( c. \$1 T notional CDOs issued in 2006 and 2007) and complexity ( e. g. cash CDOs with 10,000 page contracts and no formal pricing)
- Their **uses** have been both **good** and **bad!**
- The **ABS markets are reviving**
- The **cash CDO market** has totally **collapsed**
- The **synthetic CDO market** has **declined**
- Swaps and CDS contracts are being moved to **cleared exchanges** and all **OTC contracts severely regulated** with **substantial reductions in dealing profits**



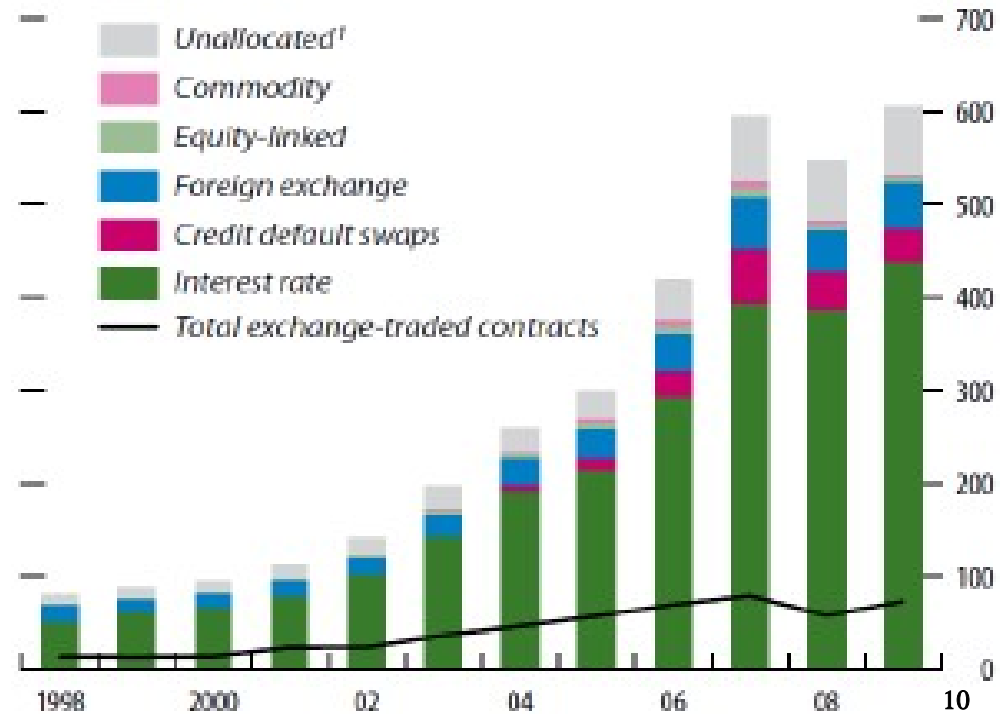
# Asset Value Proportions of 2009 Global GDP

▪ Derivatives (notional)	1012%	\$ 600 T	80%
▪ Debt & ABS	129%	\$ 77 T	10%
▪ Broad Money	115%	\$ 69 T	9%
▪ Money	9%	\$ 5 T	1%



# Global OTC Derivatives Markets

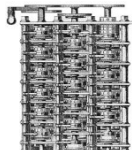
(In trillions of U.S. dollars; notional amounts of contracts outstanding)



Source: Bank for International Settlements.

Note: Over-the-counter data through June 2009; exchange-traded data through December 2009.

<sup>1</sup>Includes foreign exchange, interest rate, equity, commodity, and credit derivatives of nonreporting institutions.



# Current Derivative Valuations

**Table 19: Amounts outstanding of over-the-counter (OTC) derivatives**

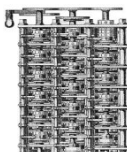
By risk category and instrument

BIS Semiannual Report (2013)

In billions of US dollars

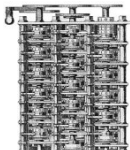
Risk Category / Instrument	Notional amounts outstanding					Gross market values				
	Dec 2010	Jun 2011	Dec 2011	Jun 2012	Dec 2012	Dec 2010	Jun 2011	Dec 2011	Jun 2012	Dec 2012
<b>Total contracts</b>	<b>601,046</b>	<b>706,884</b>	<b>647,777</b>	<b>639,366</b>	<b>632,579</b>	<b>21,296</b>	<b>19,518</b>	<b>27,278</b>	<b>25,392</b>	<b>24,740</b>
<b>Foreign exchange contracts</b>	<b>57,796</b>	<b>64,698</b>	<b>63,349</b>	<b>66,645</b>	<b>67,358</b>	<b>2,482</b>	<b>2,336</b>	<b>2,555</b>	<b>2,217</b>	<b>2,304</b>
Forwards and forex swaps	28,433	31,113	30,526	31,395	31,718	886	777	919	771	803
Currency swaps	19,271	22,228	22,791	24,156	25,420	1,235	1,227	1,318	1,184	1,247
Options	10,092	11,358	10,032	11,094	10,220	362	332	318	262	254
<b>Interest rate contracts</b>	<b>465,260</b>	<b>553,240</b>	<b>504,117</b>	<b>494,427</b>	<b>489,703</b>	<b>14,746</b>	<b>13,244</b>	<b>20,001</b>	<b>19,113</b>	<b>18,833</b>
Forward rate agreements	51,587	55,747	50,596	64,711	71,353	206	59	67	51	47
Interest rate swaps	364,377	441,201	402,611	379,401	369,999	13,139	11,861	18,046	17,214	17,080
Options	49,295	56,291	50,911	50,314	48,351	1,401	1,324	1,888	1,848	1,706
<b>Equity-linked contracts</b>	<b>5,635</b>	<b>6,841</b>	<b>5,982</b>	<b>6,313</b>	<b>6,251</b>	<b>648</b>	<b>708</b>	<b>679</b>	<b>645</b>	<b>605</b>
Forwards and swaps	1,828	2,029	1,738	1,880	2,045	167	176	156	147	157
Options	3,807	4,813	4,244	4,434	4,207	480	532	523	497	448
<b>Commodity contracts</b>	<b>2,922</b>	<b>3,197</b>	<b>3,091</b>	<b>2,994</b>	<b>2,587</b>	<b>526</b>	<b>471</b>	<b>481</b>	<b>390</b>	<b>358</b>
Gold	397	468	521	523	486	47	50	75	62	53
Other commodities	2,525	2,729	2,570	2,471	2,101	479	421	405	328	306
Forwards and swaps	1,781	1,846	1,745	1,659	1,363					
Options	744	883	824	812	739					
<b>Credit default swaps</b>	<b>29,898</b>	<b>32,409</b>	<b>28,626</b>	<b>26,931</b>	<b>25,069</b>	<b>1,351</b>	<b>1,345</b>	<b>1,586</b>	<b>1,187</b>	<b>848</b>
Single-name instruments	18,145	18,105	16,865	15,566	14,309	884	854	958	715	527
Multi-name instruments	11,753	14,305	11,761	11,364	10,760	466	490	628	472	321
of which index products	7,476	12,473	10,514	9,731	9,663					
<b>Unallocated</b>	<b>39,536</b>	<b>46,498</b>	<b>42,610</b>	<b>42,057</b>	<b>41,611</b>	<b>1,543</b>	<b>1,414</b>	<b>1,976</b>	<b>1,840</b>	<b>1,792</b>
<b>Memorandum Item:</b>										
Gross Credit Exposure						<b>3,480</b>	<b>2,971</b>	<b>3,912</b>	<b>3,668</b>	<b>3,626</b>

c. 6% global GDP



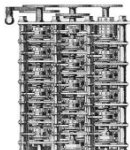
# Cui Bono? Whose Risk Is It Anyway?

- Hedging **bank** interest rate and forex **strategies** with **swaps**
- Managing **banks'** counterparty risk with **cross-border** leasing deals incorporating **credit default swaps**
- Who's insuring whom? – **collateralized debt obligations** (CDOs) in the retail market
- Playing poker against the client – **swaps** with issuers' **cancellation rights** and **CDOs** with issuers' **substitution rights'**

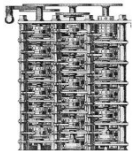


# Different Rules for Derivatives?

- **Structured derivatives** which lead to problems are not directly comparable with normal market commodities because they tend to be **individually customized** and thus largely **outside the purview of** the ideal market mechanism – namely **open price competition** in which **caveat emptor** applies
- **Pricing over-the-counter (OTC) structured derivatives** is usually **beyond the scope of** anyone other than investment banks or **specialist corporations**
- Thus in modern financial markets there may be many situations where **clients** are **in principle unable to apply pricing competition**
  - This is recognized by **regulatory measures** such as the **division of clients** into *retail, professional* and *eligible counterparty* and concepts such as **(non-)complex instruments** (MiFiD and Dodd-Frank)
- But the **implications** have **not so far** been adequately **recognized by courts**

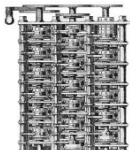


# 3. Cost of OTC Derivatives to Clients



# Caveat Emptor Revisited

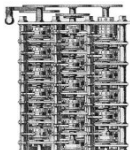
- It has been said that 30% of OTC derivatives are bought and 70% are sold (recently revised to 20 vs. 80%)
- Meaning that only 30% of deals are between counterparties who are professionally able to assess the risks involved while 70% involve counterparties who have no idea of what they are buying
- A rule of thumb is that such a counterparty should never accept a restructuring of an existing losing deal but rather cut their losses then and there





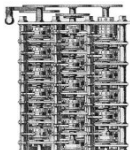
# Representative OTC Derivative Deals

- Issued by banks in the 2004-2006 boom period through the crisis to the **present** with deals issued last year and this
- Deals with maturities from 6 months to indefinite (*consol bonds*)
- Clients are **governments, second tier banks, SME's, local authorities** and **wealthy individuals** in Europe and the UK
- Contracts involve **structured** versions of **swaps, bonds** raising capital for financial institutions and **foreign exchange (FX) hedging** programmes
- Representation of the **risks** involved to clients is typically stated as **“unlimited”** and/or **ignores** egregious features of the contract structuring like *one-sided cancellation options without compensation*  
Dempster, Medova & Roberts (2011)



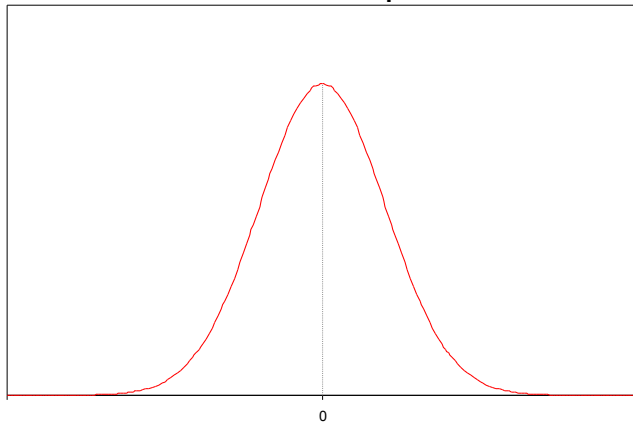
# Stylized Features of OTC Derivative Deals

- Each deal represents a **play** by the issuing bank that exploits their superior knowledge of possible **future market evolution** relative to the client's
- Issuers are usually the **client's commercial bank** and the term sheets/contracts usually bear a **feminine bank signature**
- Often the **bank requires** the **deal** as a **condition** of a **loan, refinancing** or **bond flotation**
- Most recently loan rollovers contain **"embedded" derivatives** which charge the borrower the high break costs of the bank's **possibly nonexistent** interbank market risk **hedge**
- Each deal is structured to have the enticement of a **short term** client **"sweetener"** which can **sometimes** be very **subtle**
- Often enticement can be buried in a **programme** of successive **similarly structured deals** which only in the **latter stages** become **egregious** – playing the "fish"
- Due to severe **asymmetry of information** the client is in no position to understand the **relative risks to client and bank** which are often **extreme** for the client
- When a deal begins to go wrong for the client the bank offers to postpone the agony by **restructuring** the deal(s) to one **even worse!**

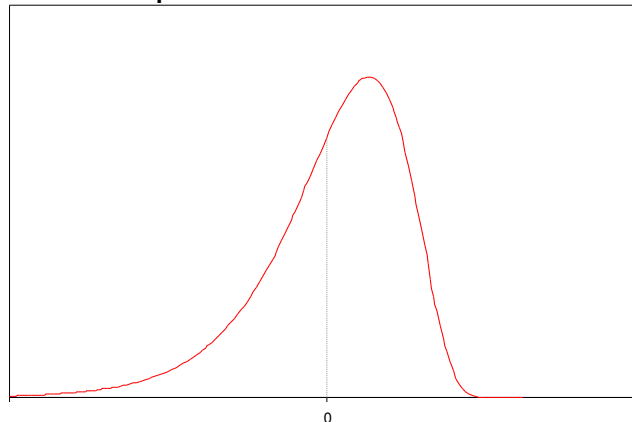


# Swap NPV Distributions

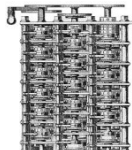
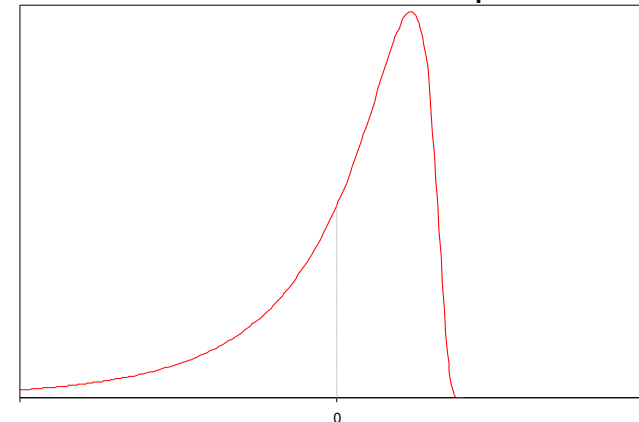
Par Swap



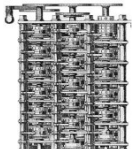
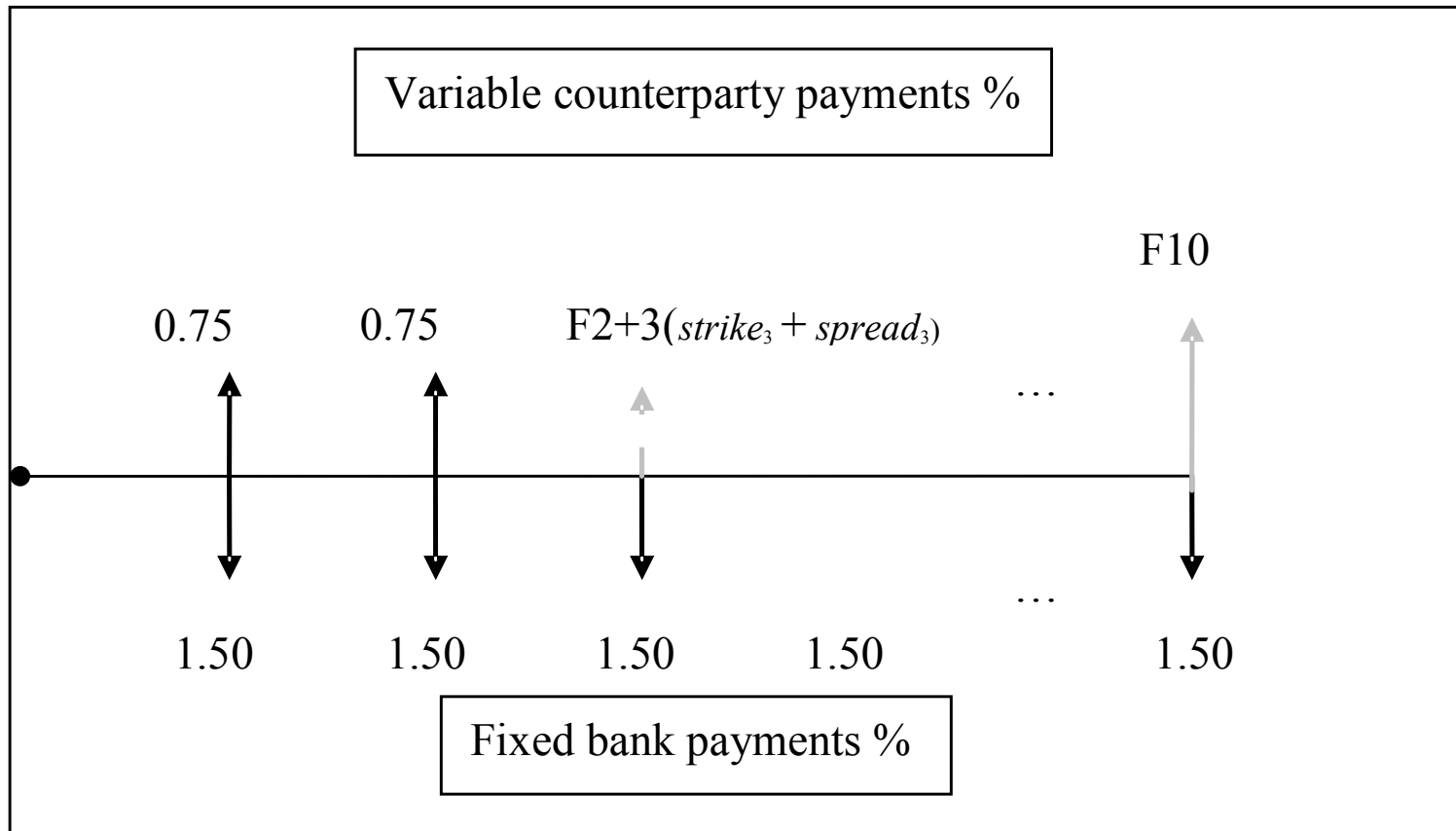
Swap with Bank Cancellation



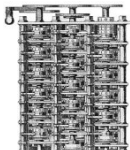
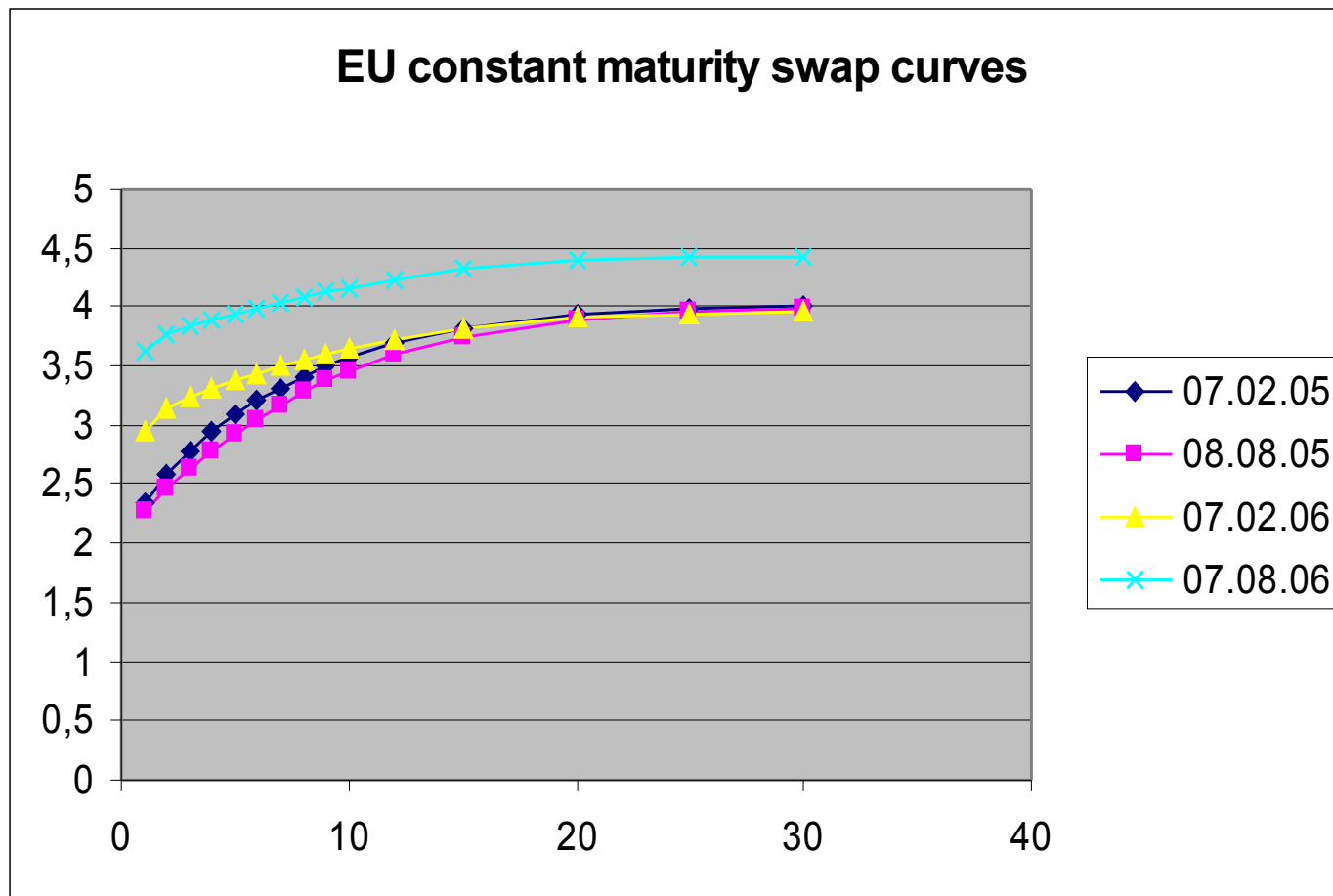
Euribor Ladder Swap



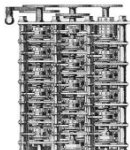
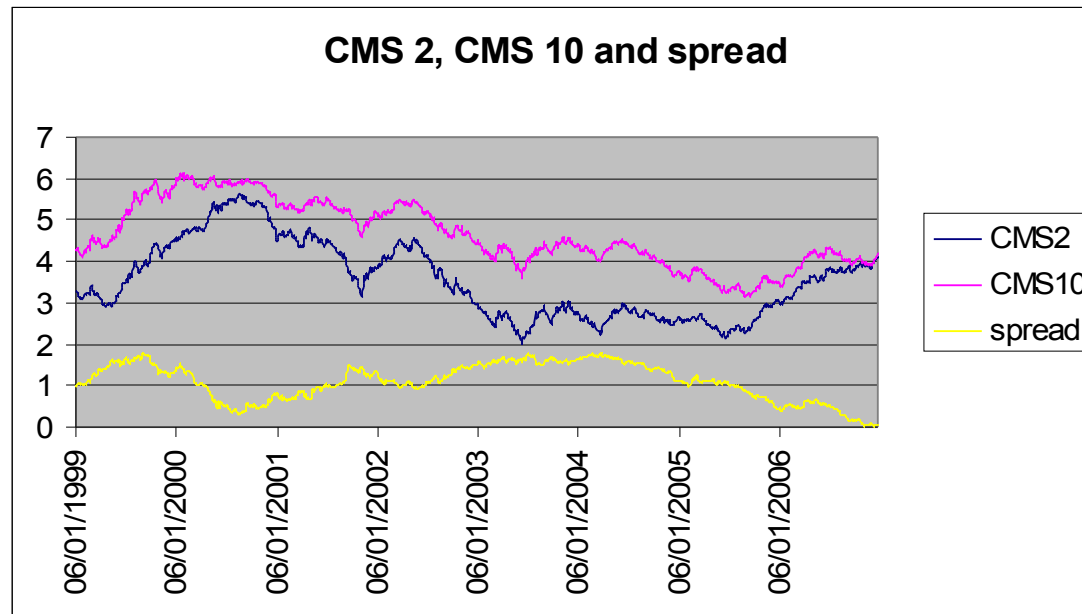
# CMS Spread Ladder Swap



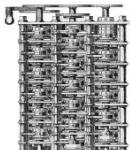
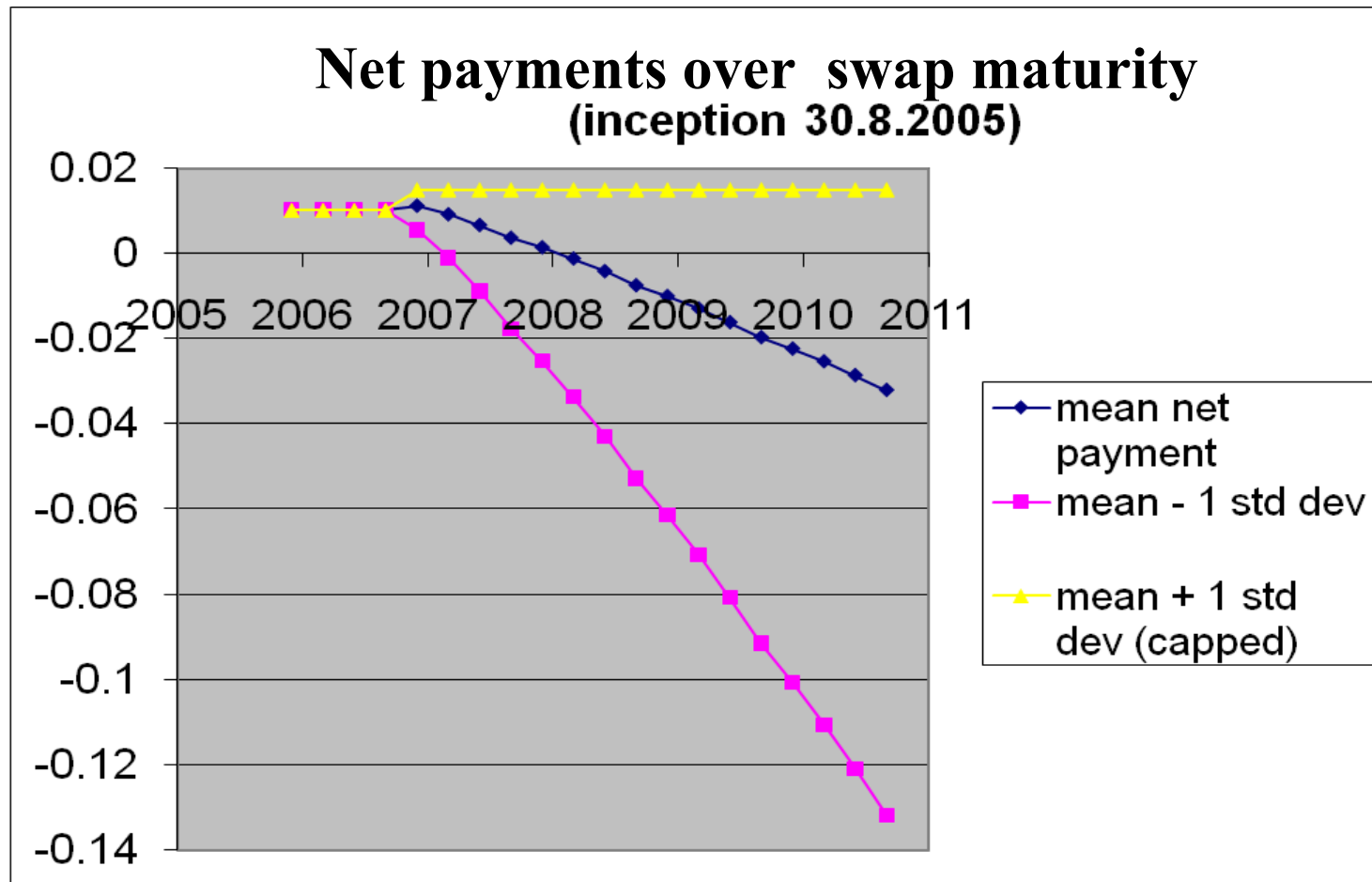
# Play on the Flattening Yield Curve



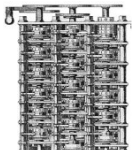
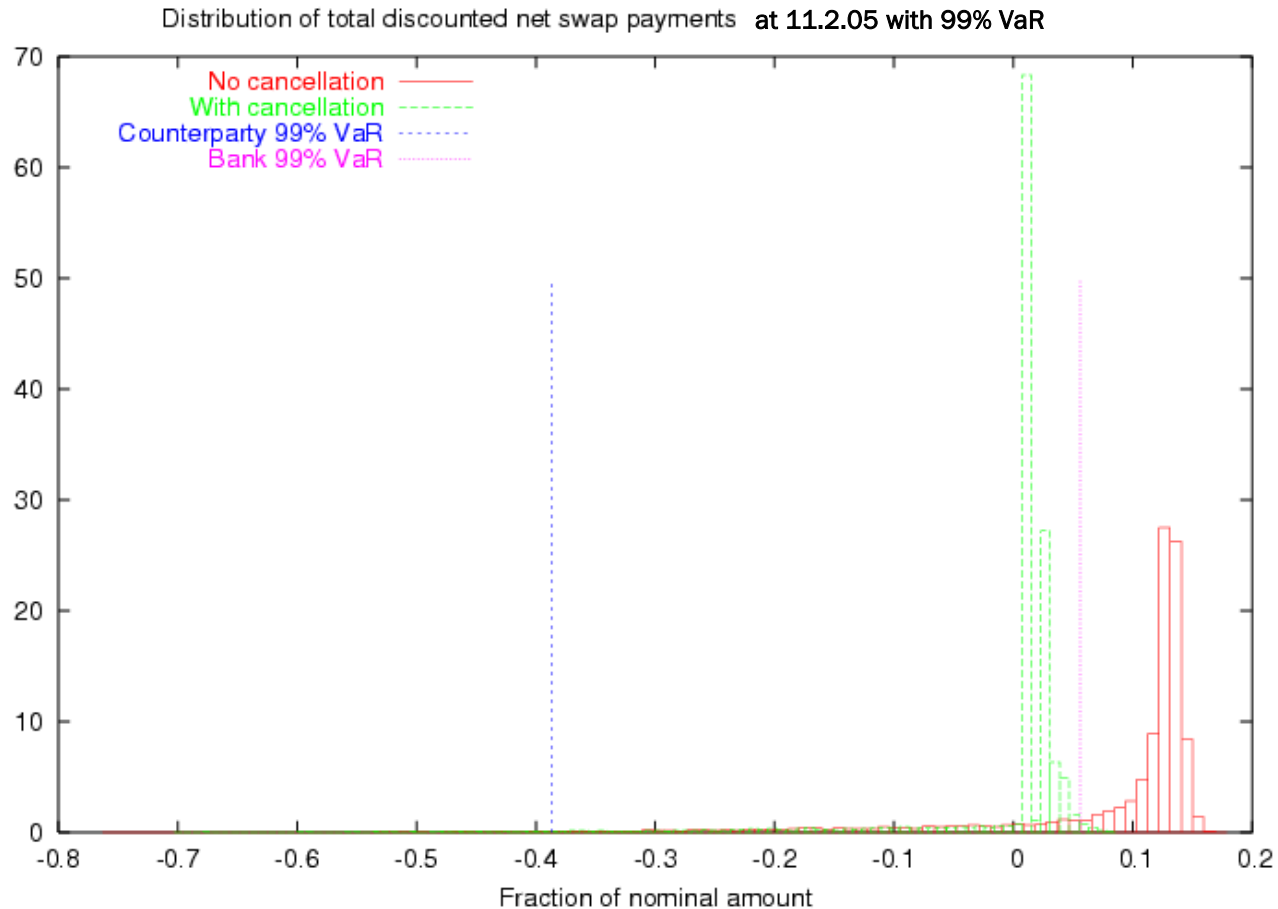
# Play on Declining Spread From Increasing Short Rates



# Declining Spread Increases Client Payments

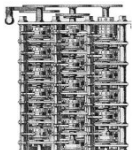
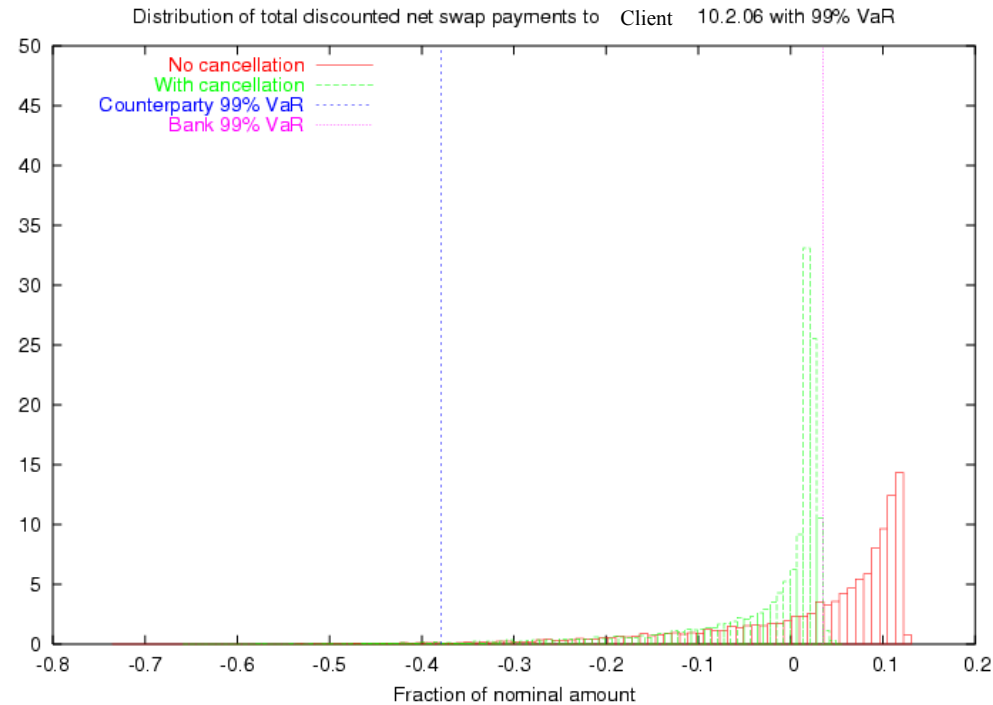


# To Result in Serious Potential Losses

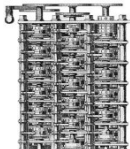
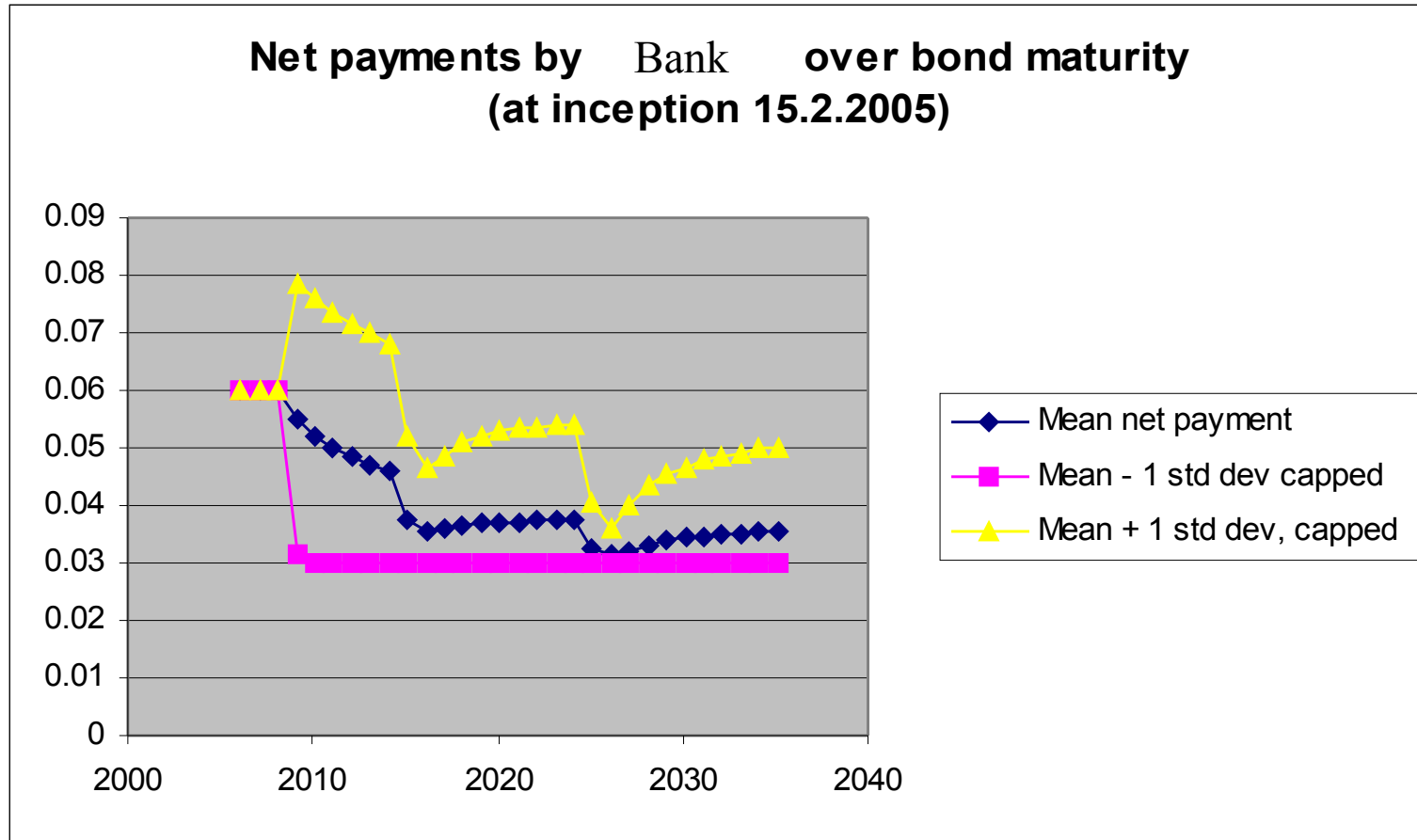




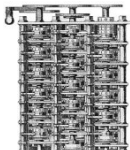
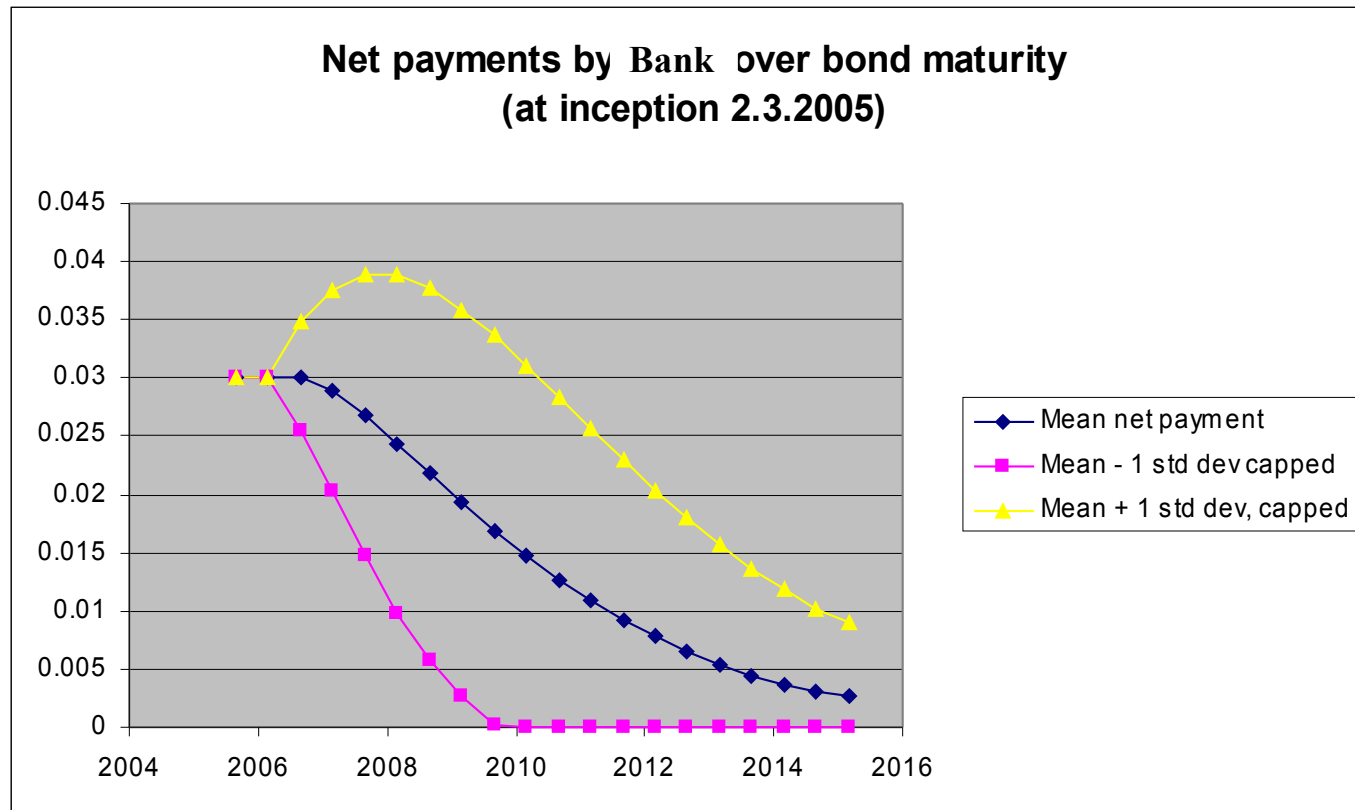
# Which Just Get Worse



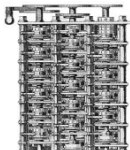
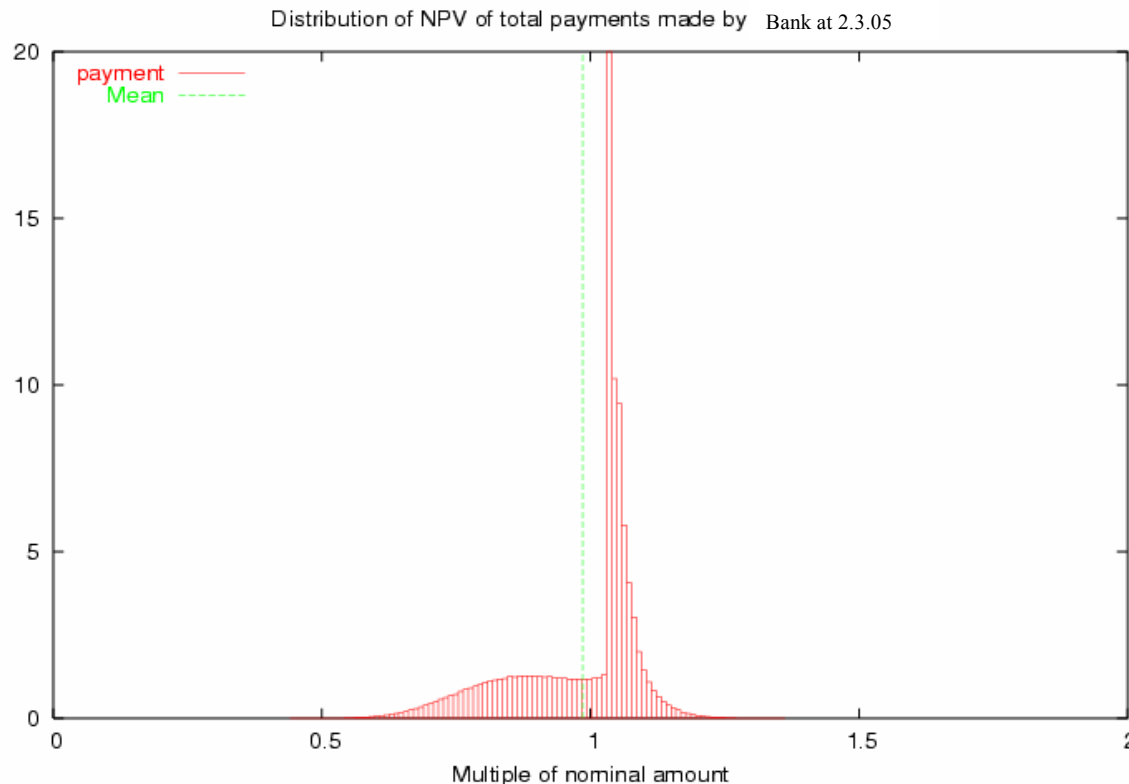
# Structured Capital Raising Callable Bond Coupons



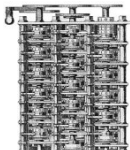
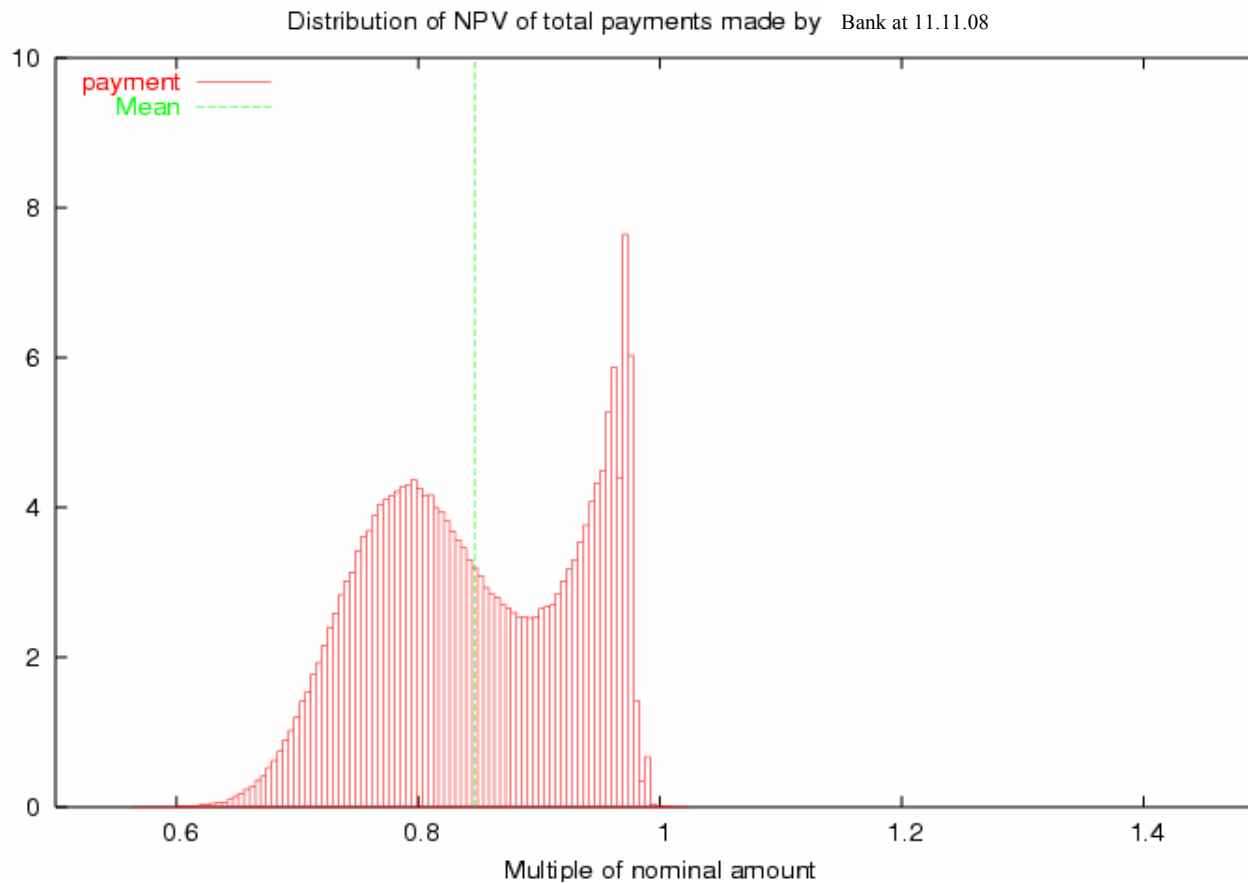
# Worse With No Floor



# Discounted PV of Callable Bond Cash Flows at Inception

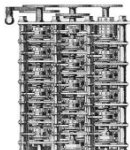


# Which Gets Worse Over Time

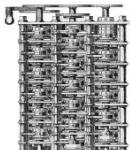
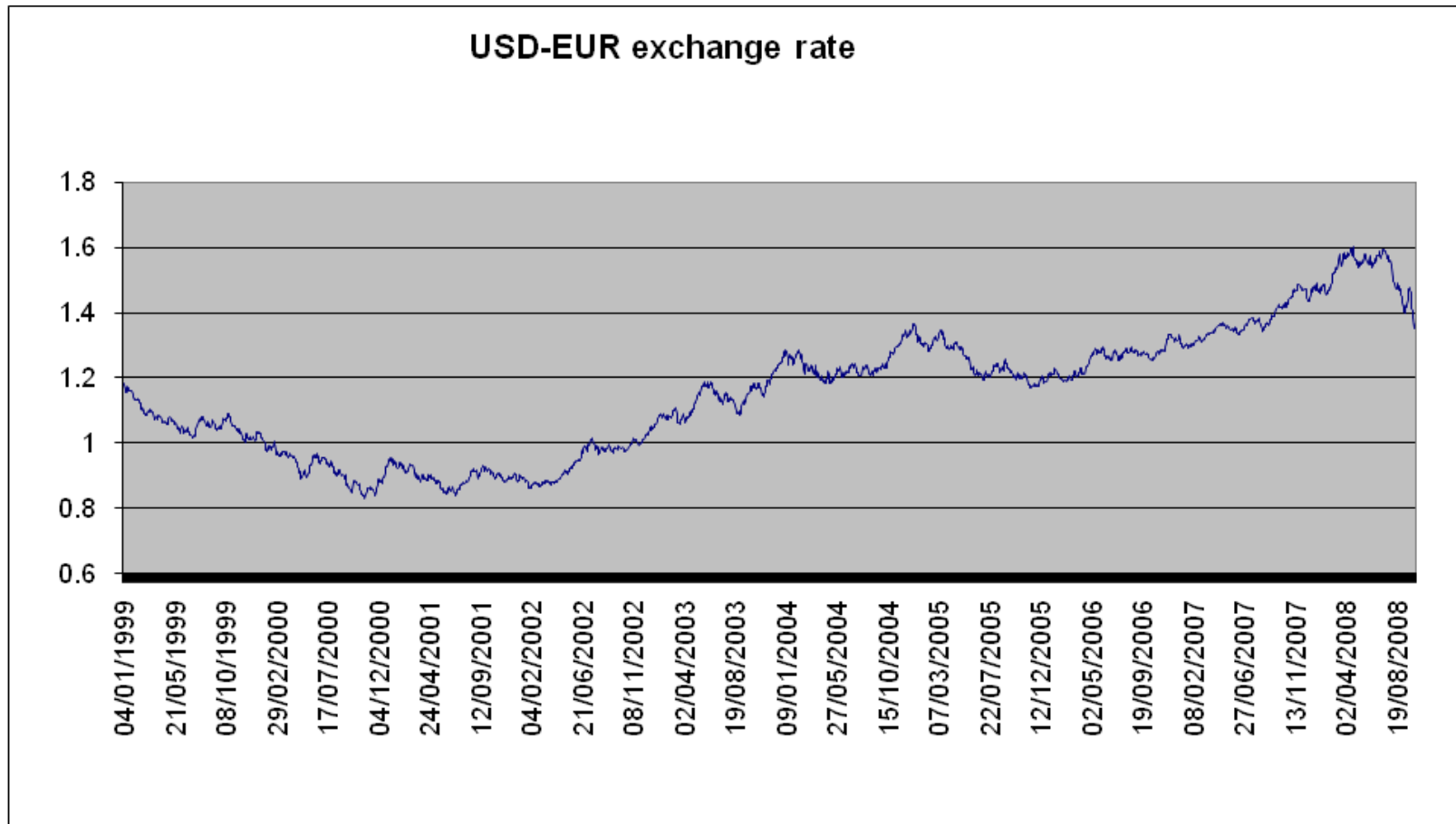


# Client FX Hedging Programme

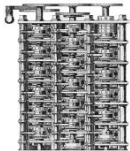
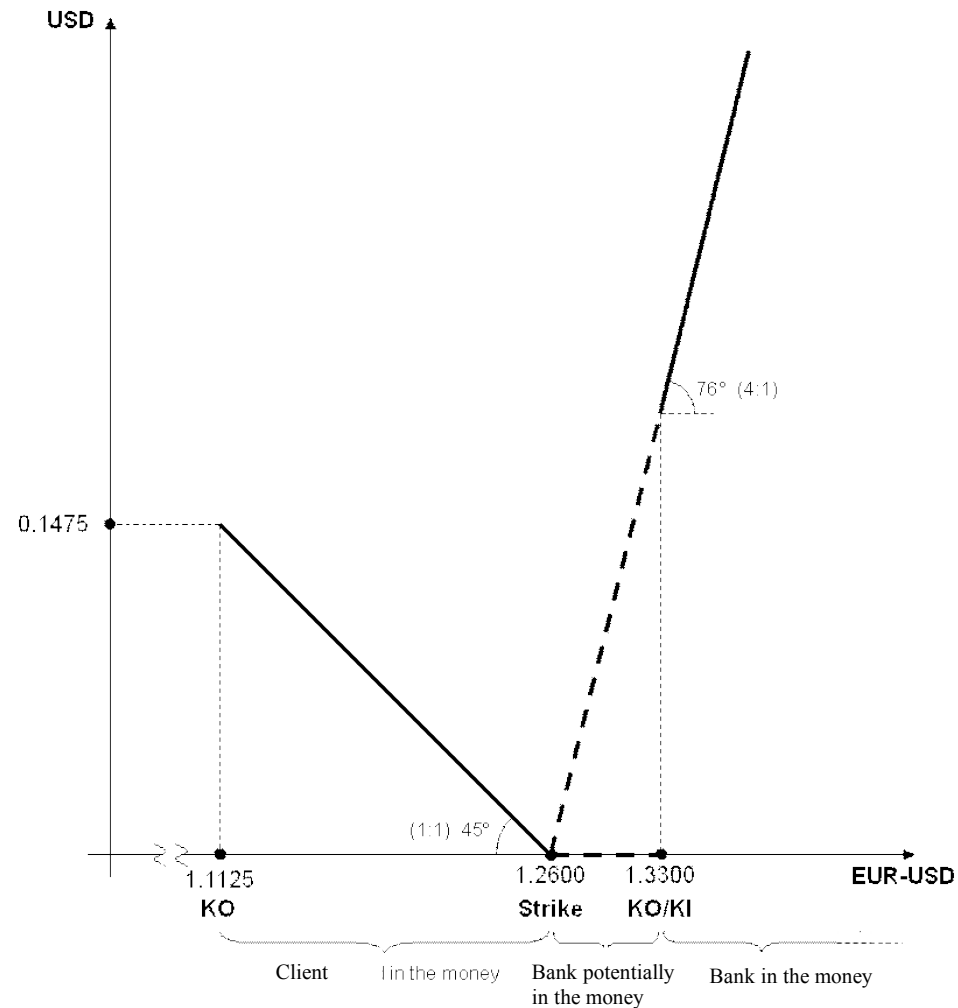
- **Over 70 option pairs** over a 33 month period in which 26 struck between March 2007 and February 2008 resulted in *substantial losses*
- **Mispricing** of both paired options involving *negative smile corrections*
- **Multiple restructurings** *incorporating losses in notional* and *improving knock-in points* for bank amounting to 28% of client losses
- **Contract exercise changes** involved in a total of € 30.5 M losses on 26 losing deals which were billed over 5 days to the client when some *European options* had *not yet expired*



# USD-EUR Evolution

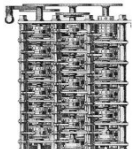
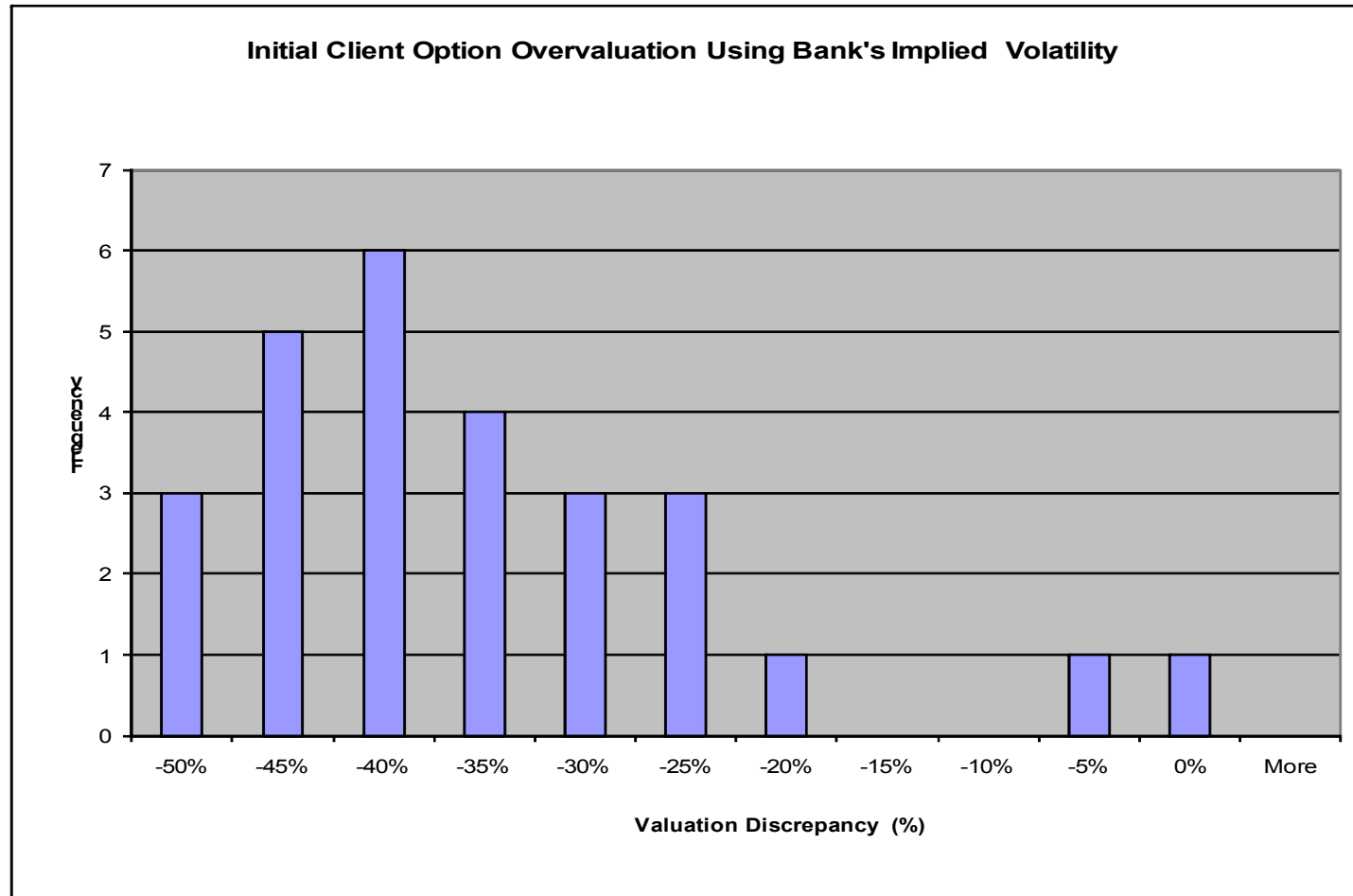


# 4:1 Asymmetric Option Pair Payoffs (Later 6:1)



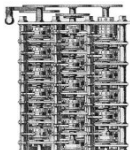


# 36% Average Initial Client Option Overvaluation

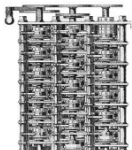
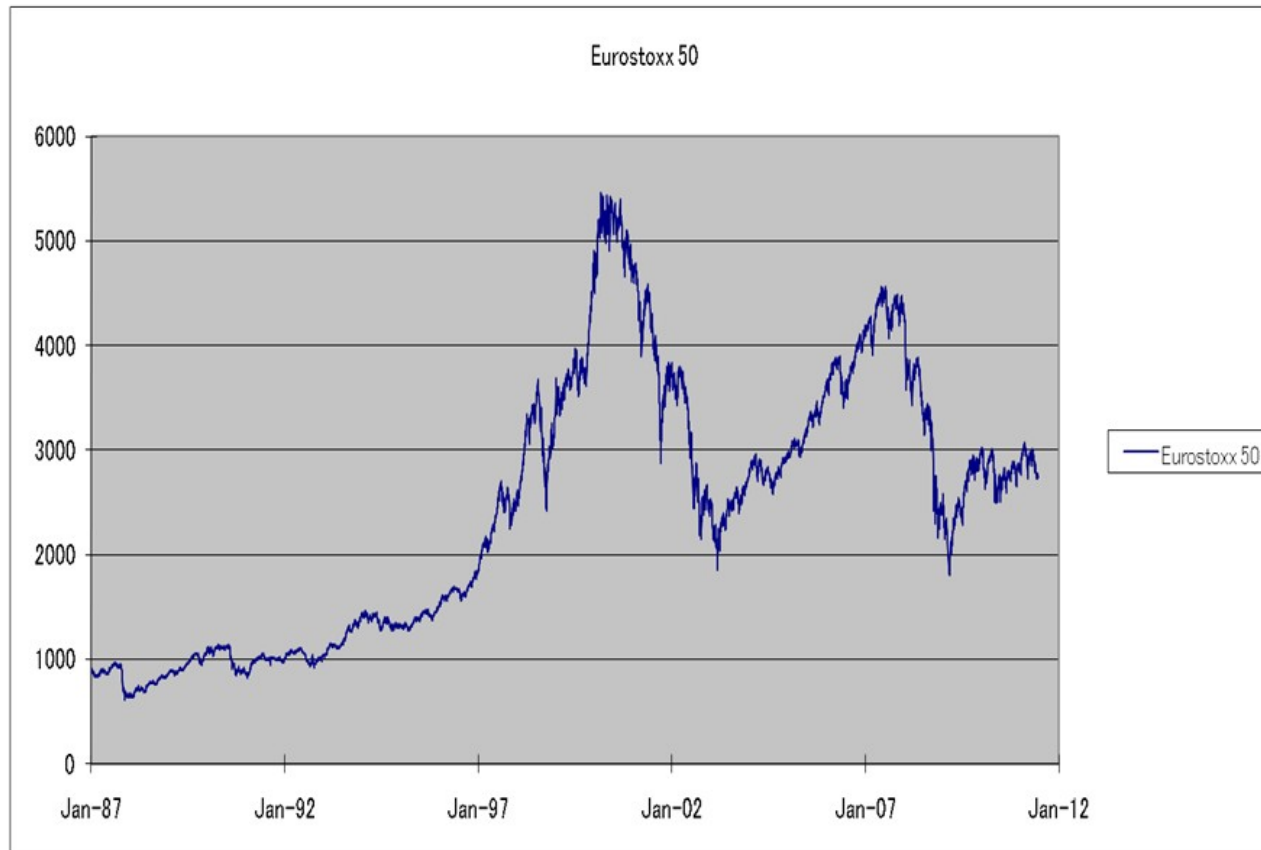


# Bank Plays Seen More Recently

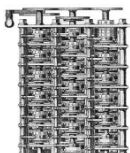
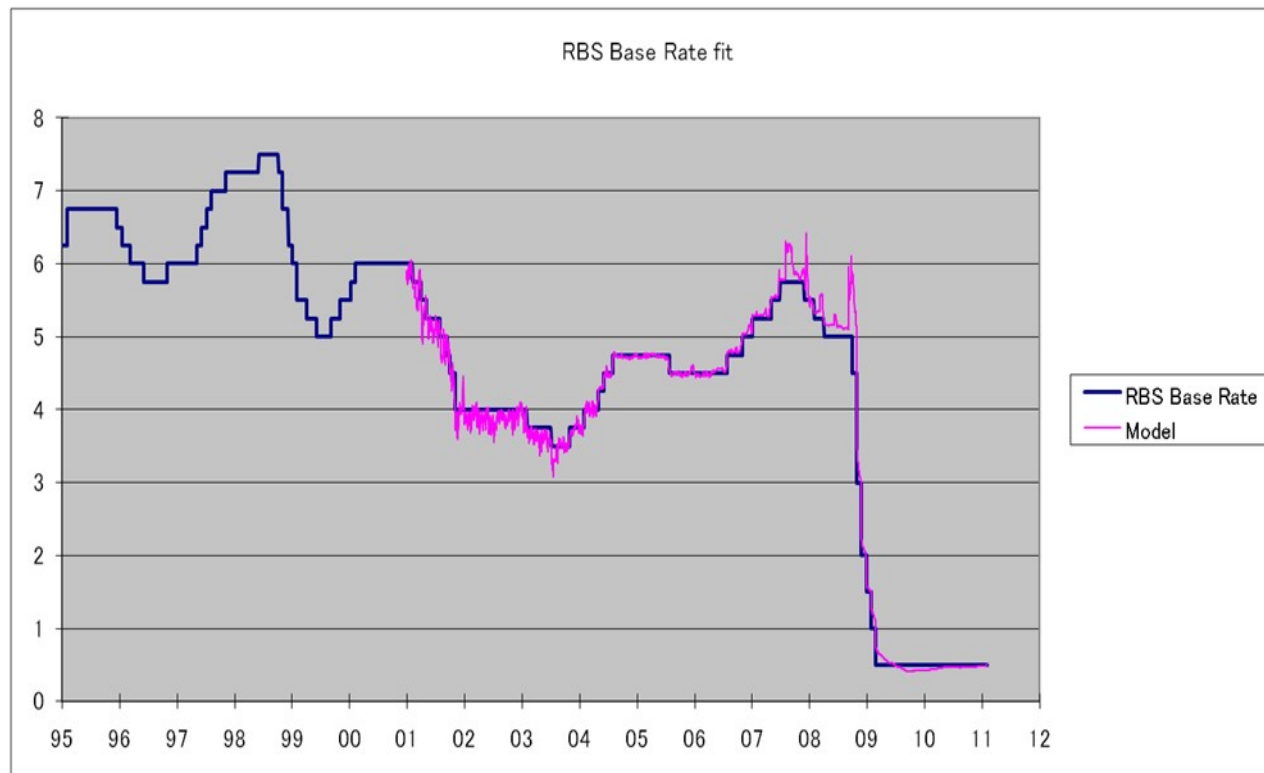
- As Lehman's and other bank's positions worsened over 2008 and short rates dropped precipitously CMS spread ladder swaps began to be based on **yield curve steepening**
- Projected **drops in the Eurostoxx50** as the crisis deepened based on earlier internet bubble behaviour of the index
- UK banks sold vanilla fixed floating swaps to retail customers – or **required** them as “hedges” on loans! – with no warning of the imminent **downside short rate risks**
- (Slightly) more sophisticated clients were sold **structured collars**
- Many cross currency or currency related swaps with clients were based on the **strengthening of the Swiss franc** against other currencies with the “flight to quality” as the euro crisis developed
- Projected drops in the 10 year constant maturity swap rate CMS10 as the crisis deepened with current artificially low rates due to **quantitative easing** (QE)
- Projected strengthening or currently (Abe) **weakening of the JPY-USD exchange rate** with short maturity high frequency structured **target profit forward** contracts



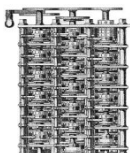
# EuroStoxx50 Evolution



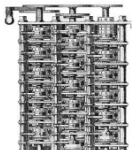
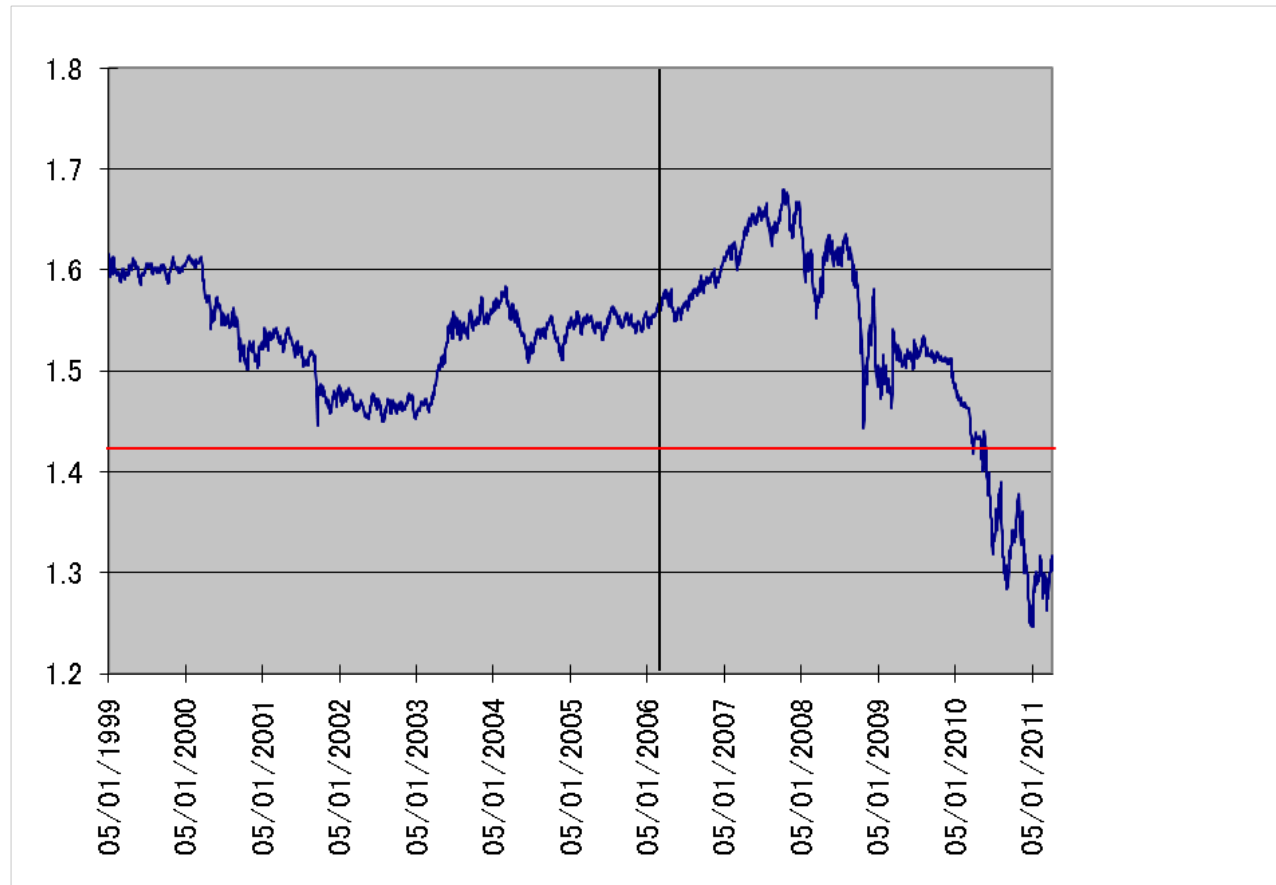
# UK Base Rate Evolution



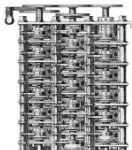
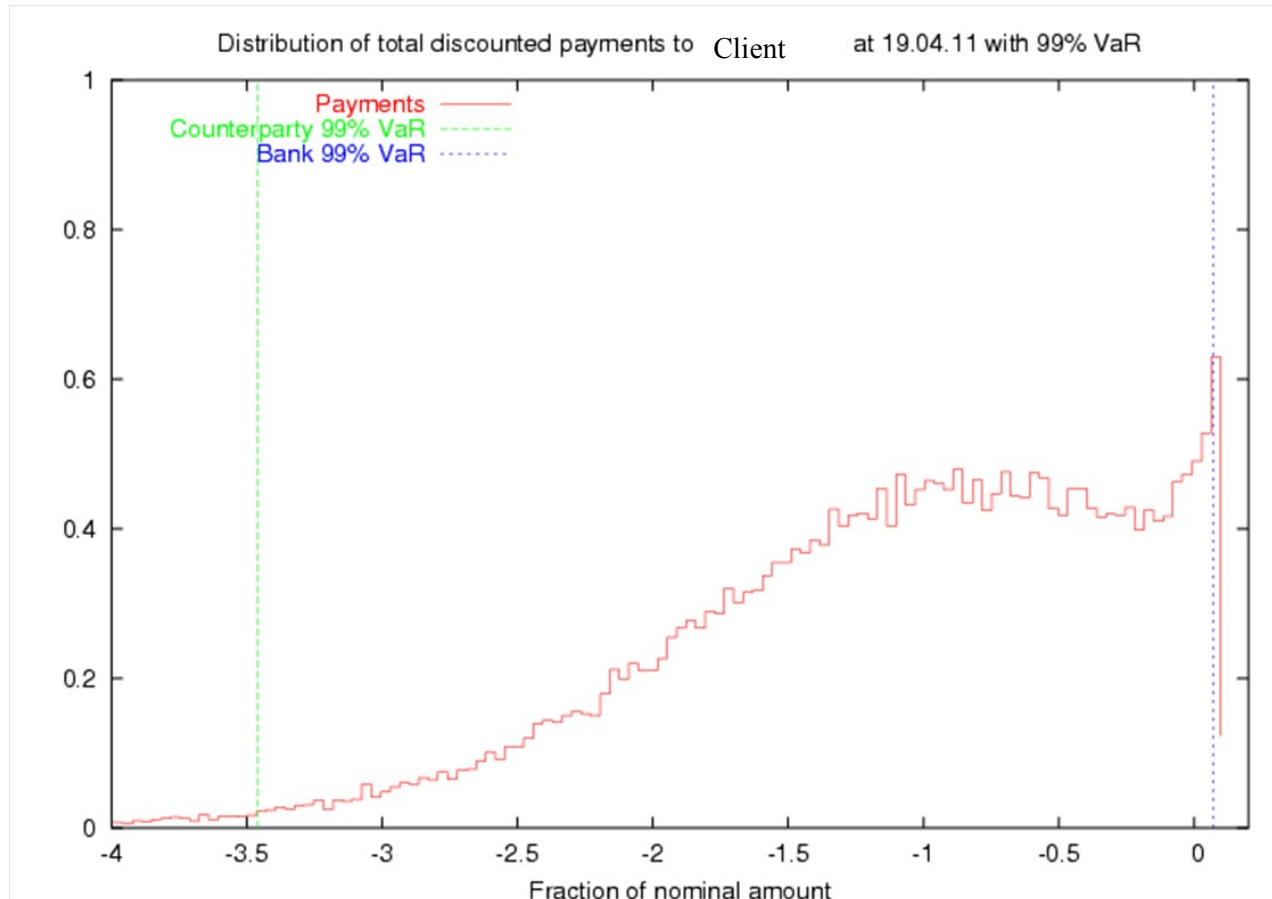
# EUR-GBP, GBP-CHF & EUR-CHF Evolution



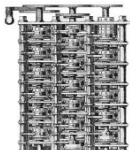
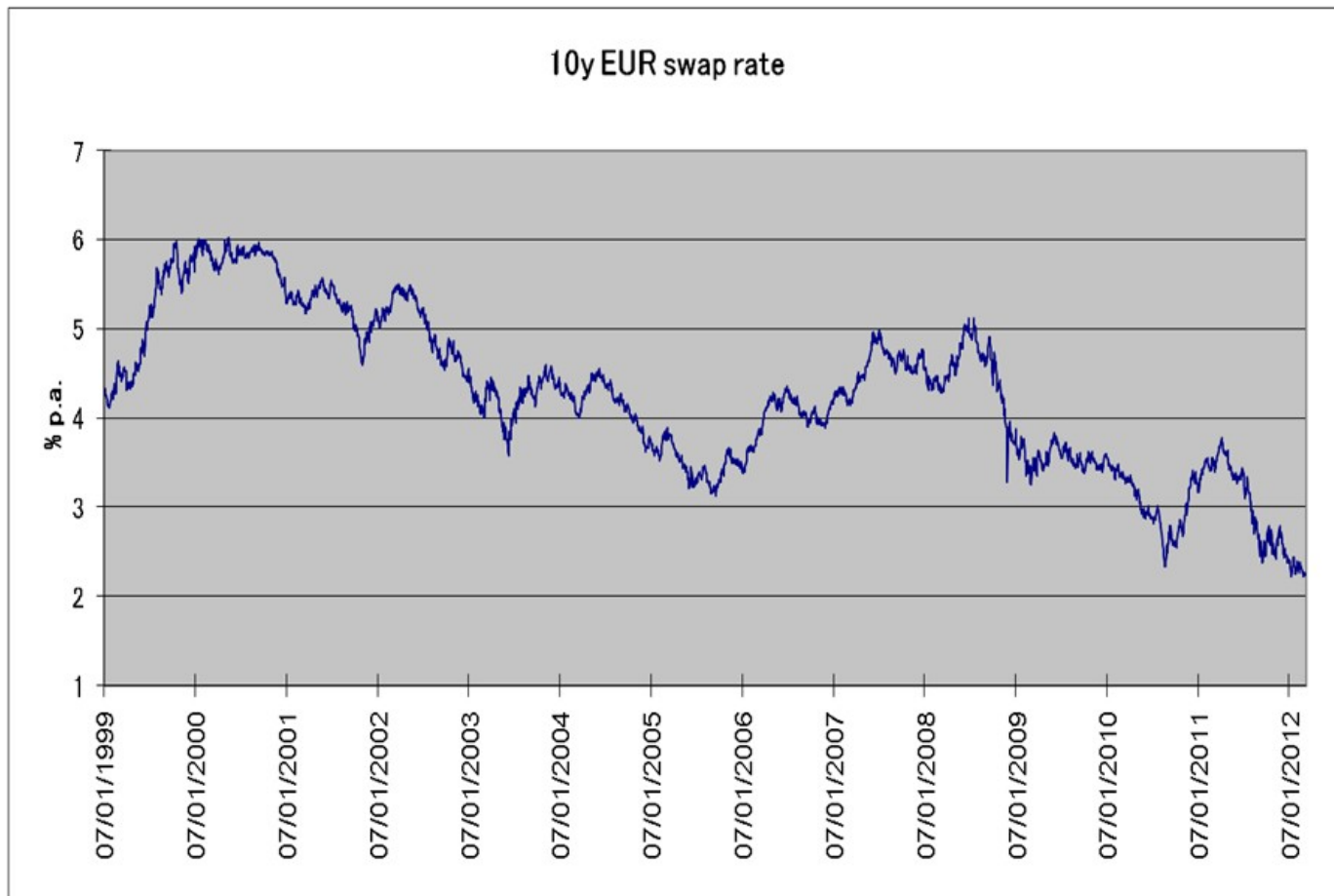
# EUR-CHF Evolution



# NPV VaR of a Restructured Currency Swap

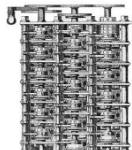
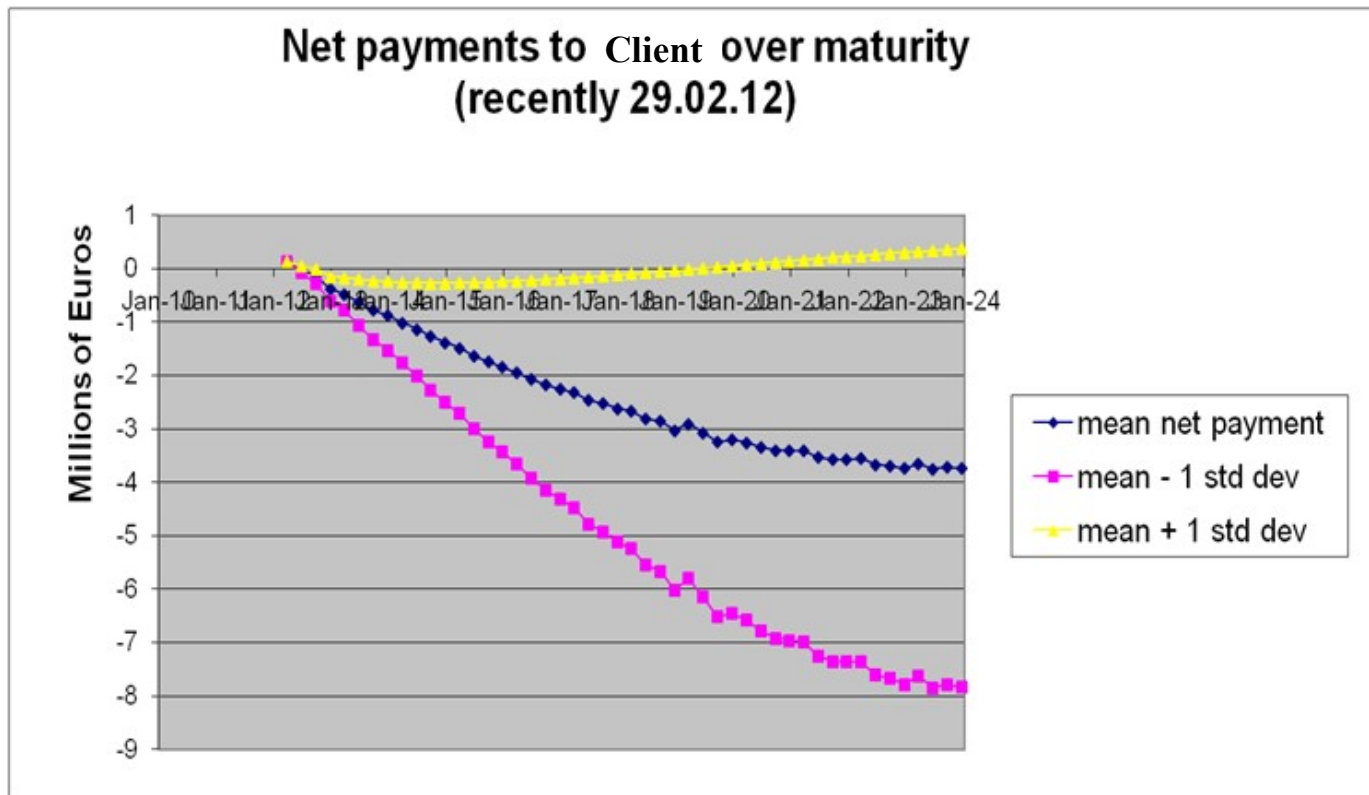


# CMS10 Rate Evolution

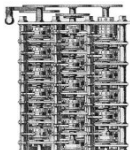
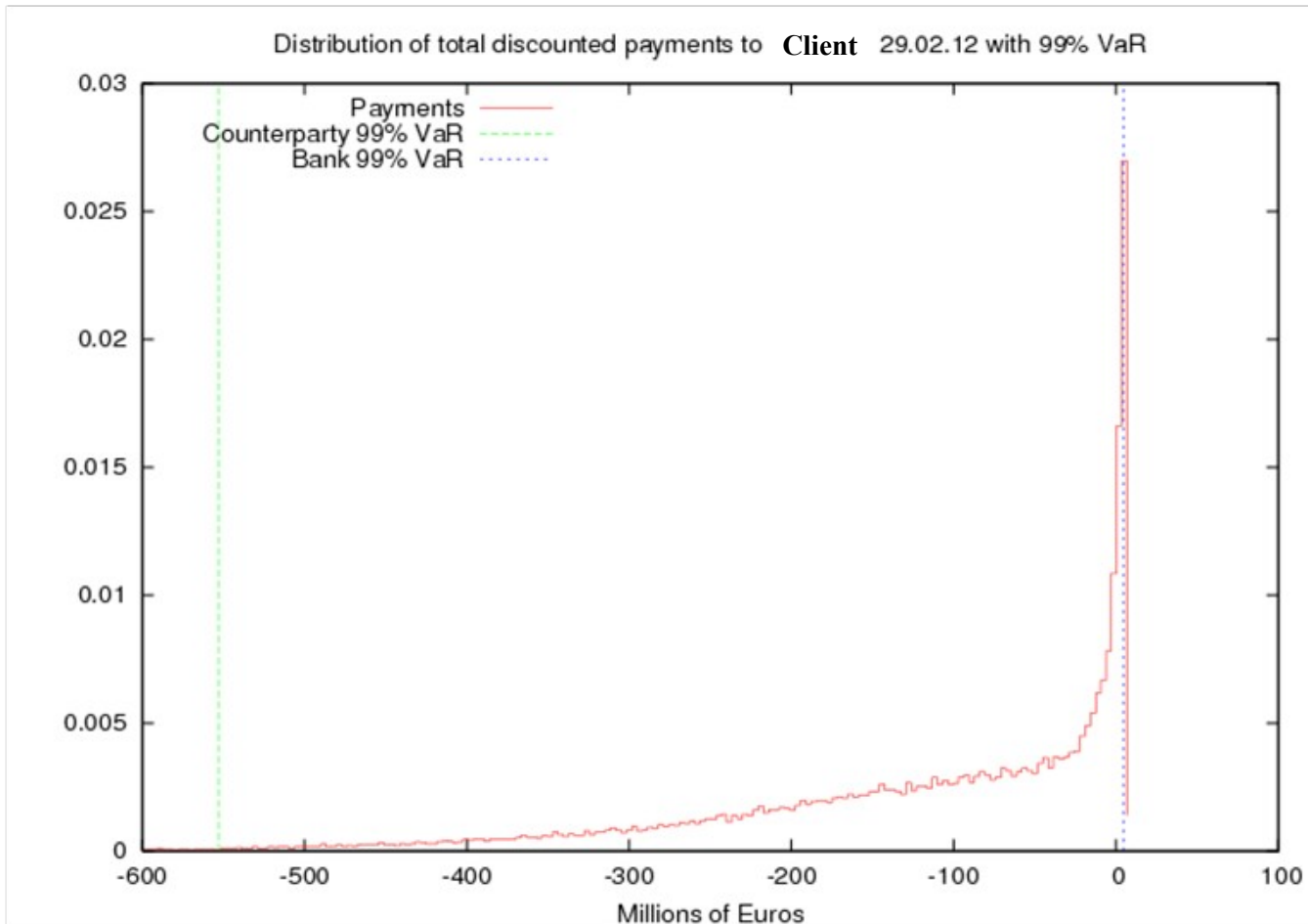




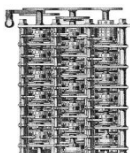
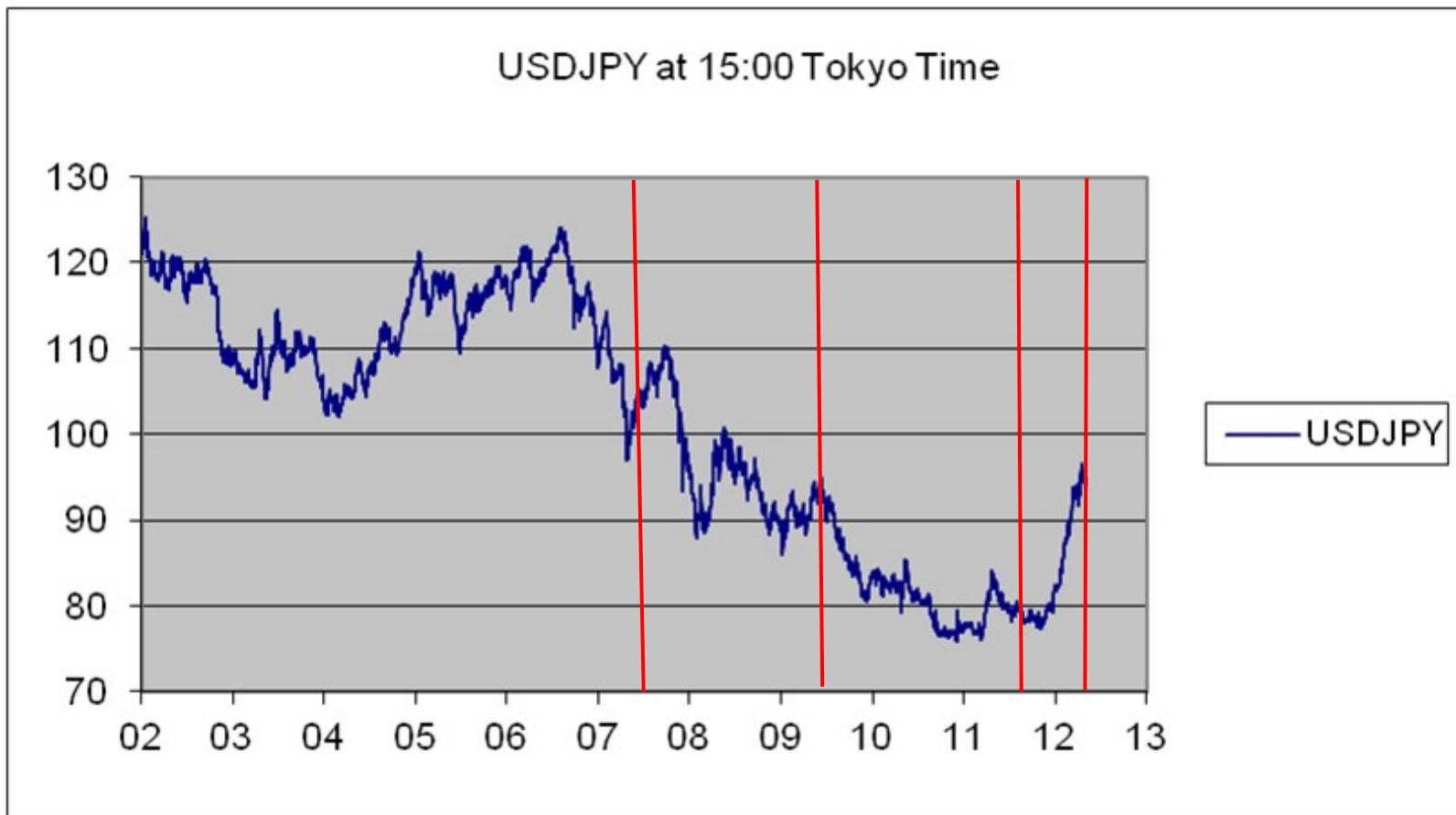
# 2<sup>nd</sup> Restructured CMS10 Memory Swap Amortised NP €10.5M



# NPV of 2<sup>nd</sup> Restructured CMS10 Memory Swap



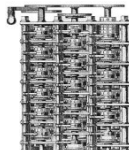
# JPY-USD Evolution



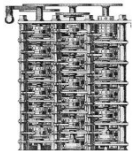
# Bank Issuance of OTC Derivative to Clients

## Summary

- Products are invariably **mispriced** in favour of the bank **at inception** and get **worse over time**
- It's like going to the track having fixed the horse race
- You are not absolutely guaranteed to win but you surely have an edge on the punters!



# 4. Pricing Methodology



# Economic Factor Model

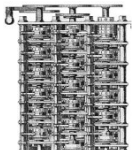
- A 3 factor **extended Vasicek** Gaussian model specified under P by

$$dX(t) = (\mu_X - \lambda_X X(t) + \gamma_X \sigma_X)dt + \sum_{j=1}^3 \sigma_{1j} dW_j(t) \quad \text{Long rate}$$

$$dY(t) = (\mu_Y - \lambda_Y Y(t) + \gamma_Y \sigma_Y)dt + \sum_{j=1}^3 \sigma_{2j} dW_j(t) \quad \text{Minus Slope}$$

$$dR(t) = \{k[\underbrace{X(t) + Y(t)}_{\text{Unobservable instantaneous short rate}} - R(t)] + \gamma_R \sigma_R\}dt + \sum_{j=1}^3 \sigma_{3j} dW_j(t)$$

- Its discretization is estimated from **GMS swap data** with **many observed** yield curve points – **rates** – from 1 day (Libor) to 30 years (Treasury) using the **EM algorithm** which iterates **Kalman filtering** and **maximum likelihood estimation** to convergence
- Specifying the **constant market prices of risk** in terms of volatility units solves the  $X$  &  $Y$  identification problem and setting them to **zero** generates the **pricing factor process**
- This workhorse model has been used for pricing complex products and ALM using daily to quarterly frequency data in US, UK, EU and Japanese jurisdictions

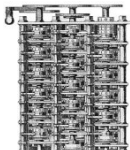


# Calibrating the EFM Model

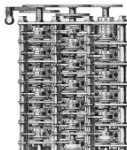
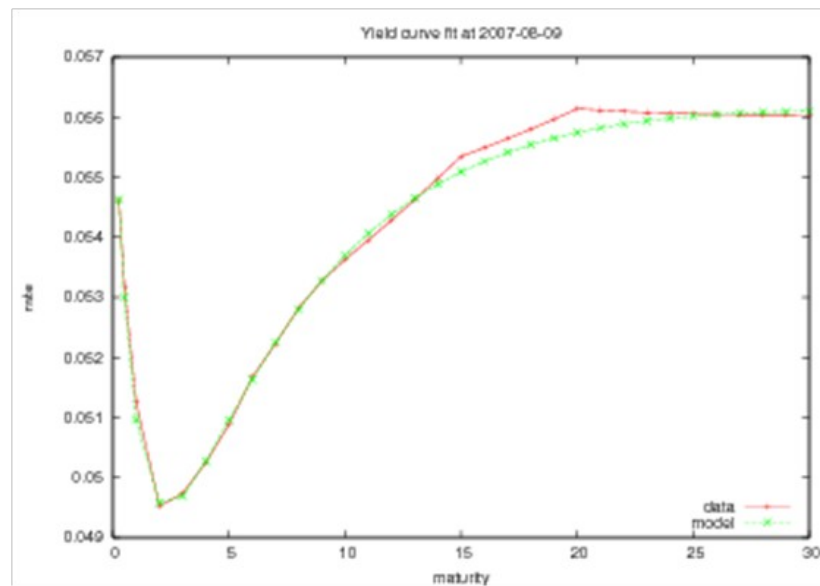
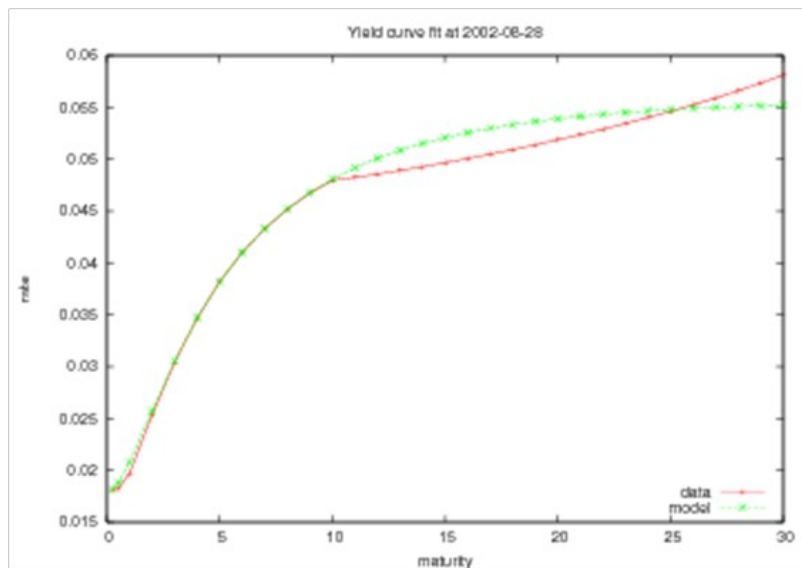
- Given the vector of **parameters**  $\theta$  this Gaussian **extended Vasicek model** has **zero coupon bond yields** for maturity  $\tau := T - t$  of the form

$$y(t, T) = \tau^{-1} [A(\tau, \theta)R_t + B(\tau, \theta)X_t + C(\tau, \theta)Y_t + D(\tau, \theta)]$$

- We **interpolate** the appropriate **swap curve linearly** to obtain swap rates at all maturities and then use 1, 3 and 6 month LIBOR rates and the swap curve to recursively **back out** a **zero coupon bond yield curve** for each day **from** the basic **swap pricing equation**
- This gives the **input data** for model calibration to give the **parameter estimates**  $\hat{\theta}$
- Calibration is accomplished using the **EM algorithm** which **iterates** successively **Kalman filtering** and **maximum likelihood estimation** from an initial parameter estimate
- At each iteration **multi-extremal likelihood** optimization in  $\theta$  is accomplished using a **global optimization** technique **followed by** a **quasi-Newton algorithm**
- The procedure is run on a Dell **44 Intel core** system using **parallelization** techniques and we are currently investigating the use of **cloud computing** for these calculations



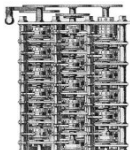
# Goodness of Fit to Historical Yield Curves



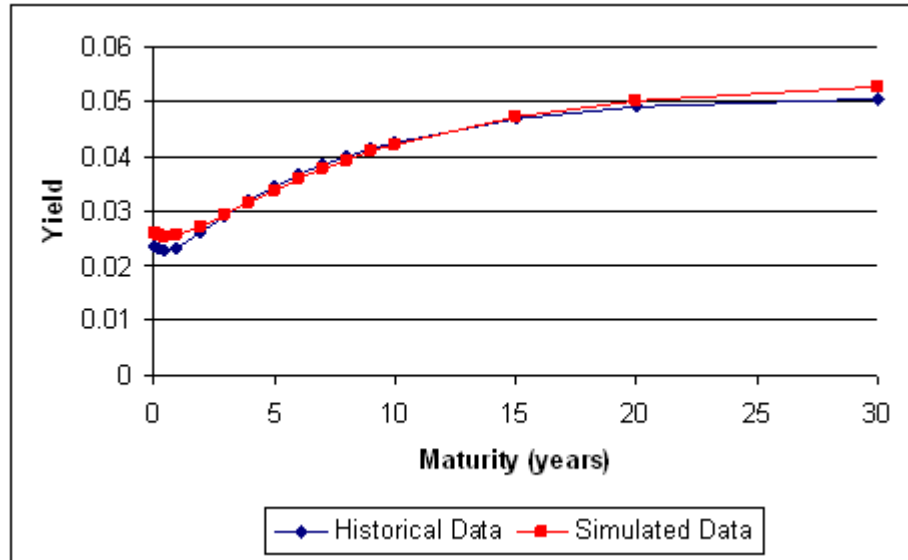


# Monte Carlo Structured Deal Valuation

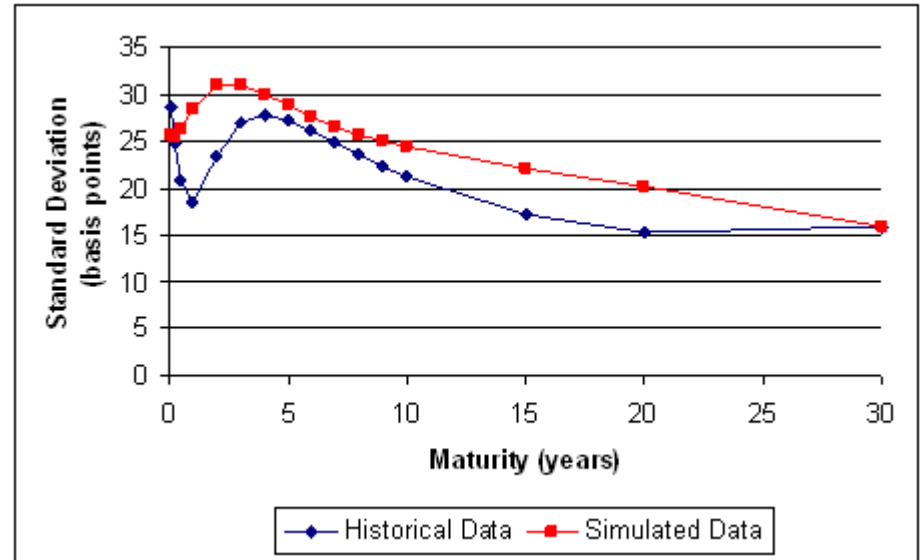
- OTC deal valuation may require *several* **yield curve estimates** together with **CMS swap rates** and **cross currency rates** which are all assumed **correlated** with *fixed* values
- The estimated **factor dynamics** of  $(\mathbf{X}, \mathbf{Y}, \mathbf{R})$  are **simulated forward** under the **Q measure** for **pricing** with the fixed market prices of risk set to 0
- The corresponding curves and FX rates are simulated to maturity together with a **daily time step** from respectively the valuation day yield curve estimates and FX data using **10,000 paths**
- For OTC client deals **optionality** is typically in the form of **bank cancellation** rights (without compensation) at prescribed dates – usually at all **reset dates** after some initial period from inception
- We use an augmented version of a **sub-optimal cancellation rule** due to **Andersen (1999)** which relies on a **score function** and cancels if
- The exercise **thresholds**  $s_t^*$  are determined by a **separate** set of **10,000 paths** for  $(\mathbf{X}, \mathbf{Y}, \mathbf{R})$  as the **discounted** value of all the **remaining net payouts** to the bank along the **average factor path**



# EFM Model EU Yield Curve Prediction 2003<sup>58</sup>



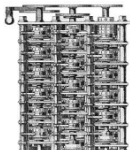
Mean level of yields over 2003 for historical and simulated weekly data



Weekly standard deviation of yields over 2003 for historical and simulated data

Dempster, Medova & Villaverde (2010)

- Longer term out-of-sample yield curve prediction has been independently found recently to be superior to the **arbitrage-free Nelson-Siegel model** of **Christensen, Diebold & Rudebusch (2009)** widely used by central banks

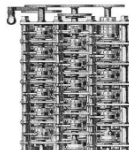


# Nonlinear 3-Factor Black Model

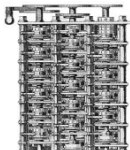
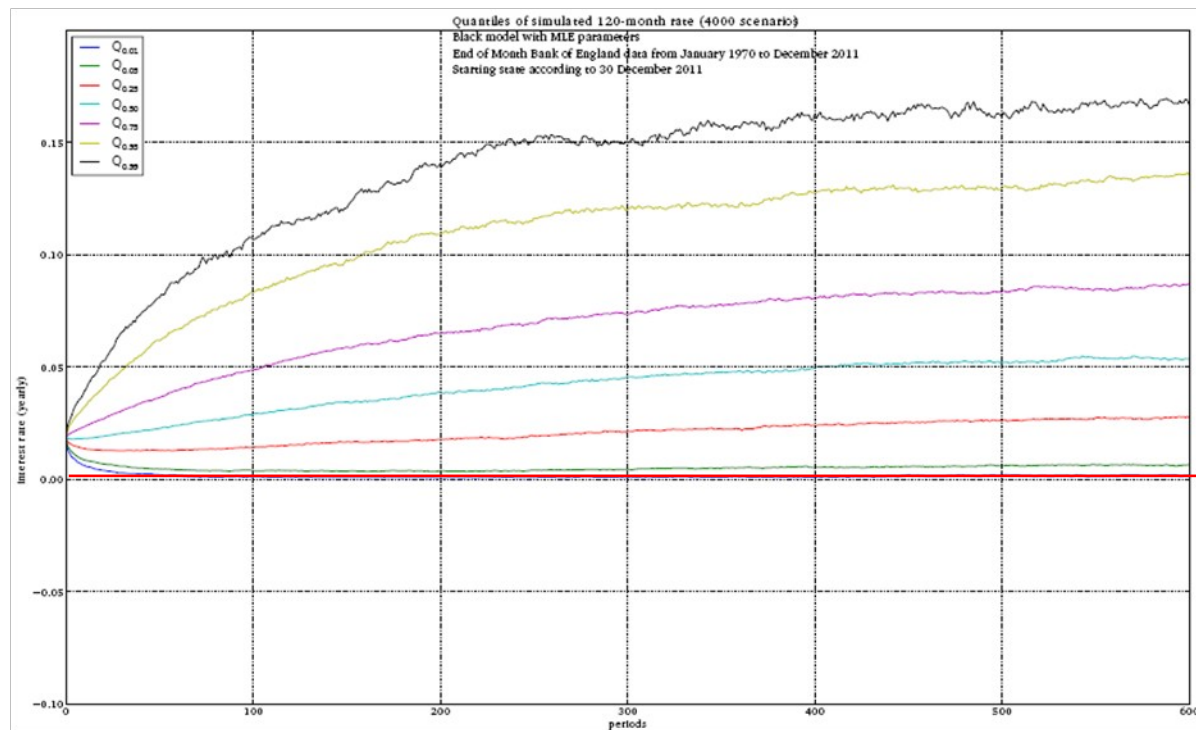
- In a posthumously published paper [Fisher Black \(1995\)](#) suggested correcting *a priori* a Gaussian short rate model for a **shadow** short rate  $r$  to give the **actual** short rate as

$$r_{actual,t} := \max[0, r_{shadow,t}]$$

- Applied to an affine 3-factor Gaussian yield curve model such as that of our EFM model or JSZ this yields a **hard nonlinear estimation** problem  
[Joslin, Singleton & Zhu \(2011\)](#)
- Such models have been studied in the 2-factor case by the Bank of Japan and Stanford but their discount bond pricing (rate) methods do not easily extend to 3 factors  
[Ichuie & Ueno \(2007\)](#)   [Kim & Singleton \(2011\)](#)   [Christensen & Rudebusch \(2013\)](#)  
[Kim & Priebsch \(2013\)](#)



# Black Model 10 Year Gilt Rate 50 Year Predicted Distribution 2011-2061

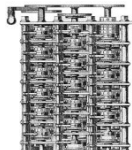


# 3-Factor Black Model Stylized Properties <sup>61</sup>

Stylized Fact Properties	Yield Curve Model					
	CIR	BDFS	Vasicek	JSZ/HW	JSZ/HW/BRW	Black
	$A_3(3)$	$A_3(3)$	$A_3(3)$	$A_1(3)$	$A_0(3)$	$A_0(3)$
Mean Reverting Rates	Yes	Yes	Yes	Yes	No	Yes
Nonnegative Rates	Yes	No	No	No	No	Yes
Stochastic Rate Volatility	Yes	Yes	No	No	No	Yes*
Closed Form Bond Prices	Yes	Yes	Yes	Yes	Yes	No
Replicates All Observed Curves	No	Yes	Yes	Yes	Yes	Yes
State Dependent Risk Premia	No	No	No	Yes	Yes	Yes
Good for Long Term Simulations	No	No	No	No	No	Yes
Slow Mean Reversion Under $Q$	No	No	No	No	No	Yes
+ve Rate/Volatility Correlation	No	No	No	No	No	Yes
Effective in Low Rate Regimes	No	No	No	No	No	Yes

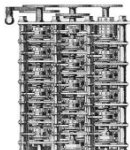
Table 1. Properties of evaluated yield curve models with regard to stylized facts

\*Rate volatilities are piecewise constant punctuated by random jumps to 0 at rate 0 boundary hitting points.



# Monte Carlo Bond Pricing

- Calibration of the **nonlinear Black model** with **any** underlying 3 factor Gaussian **shadow rate model** is **more computationally intensive** than for this underlying affine model
- Currently **cloud facilities** and Monte Carlo are used with a **JSZ 4 yield curve point model**
- In more detail:
  - For **short rates** the **closed form** numerical rate calculations of **Kim & Singleton (2011)** are used
  - For **long rates** the **averages** of Monte Carlo **forward simulated paths** -- which automatically take account of the **convexity adjustment** otherwise required for this model – are used
- With this approach filtering a **multi-curve EFM model** for **OTC structured derivative valuation** becomes **very computationally intensive**

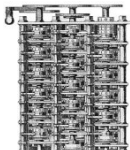


# PDE Bond Pricing

- A possible key to calibration of both the JSZ and EFM models is the efficient solution for **discount bond prices**  $P(\tau)$  of **all maturities**  $\tau$  at **each time**  $t$  of a 3-dimensional **parabolic partial differential equation** (PDE) of the form

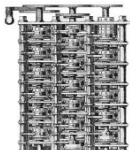
$$\partial P_t(\tau) / \partial \tau = \sum_{i,j=1}^3 a_{ij} \partial^2 P_t(\tau) / \partial y_i \partial y_j + \sum_{i=1}^3 b_i \partial P_t(\tau) / \partial y_i + c P_t(\tau)$$

- Kim and Singleton's 2-dimensional alternating direction implicit (ADI) solution method will not cope with the 3-D case  
[Kim & Singleton \(2011\)](#)     [Lipton \(2013\)](#)
- Rather than simulation-based techniques we are currently investigating applying a fast robust 3-D PDE solver based on an **interpolating wavelet-specified irregular mesh implicit** method that we have developed for complex derivative valuation  
[Jameson \(1998\)](#)     [Carton de Wiart & Dempster \(2011\)](#)



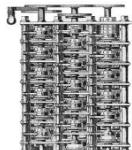
# Unscented Kalman Filter Bond Pricing

- We are also investigating **calibrating** the **Black EFM model** with our current **EM algorithm** approach with the **unscented Kalman filter** to handle the “hockey stick” nonlinearity and cloud computing **Julier & Uhlmann (1997)**
- Working with **yields** directly as we do **rather than bond prices** computed or approximated numerically from integrals of the instantaneous short rate as in the previously cited references to Black model calibration **significantly accelerates computation**
- Putting the EFM 3-factor yield curve dynamics in **state-space form** shows that the **factor state dynamics** remain **linear Gaussian** while the **Black nonlinearity** may be **directly applied to each** observed **maturity yield** in the shadow rate affine **measurement equation** – **longer maturity yields** typically need **no correction**
- With this approach the 13 **sigma point** duplicate **calculations** of the **unscented Kalman filter** at each daily time step may be mindlessly **parallelized** to handle the Black nonlinearity in essentially the **same running time as** the calibration of the underlying EFM model using basic **linear Kalman filtering**





# 5. Evolving Regulation of OTC Derivatives



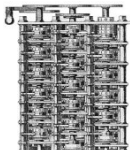
# Why Do Clients Sign OTC Contracts? Theory

- In over-the-counter markets “buyers and sellers and sellers negotiate terms privately, often in ignorance of the prices currently available from other potential counterparties and with limited knowledge of trades recently negotiated elsewhere in the market ... (illiquidity) premia are higher when counterparties are harder to find, when *sellers* have less bargaining power, when the fraction of qualified owners is smaller, and when risk aversion, volatility, or hedging demand is larger”

Based on **random search** by **rational risk neutral investors** and the **central limit theorem**  
Duffie (2012)

- Structured investment products offer **no gain after fees** to such investors and **appear** to do so only if investors **misestimate outcome likelihoods** by **overweighting favourable relative to unfavourable outcomes** – a theory of gullability?

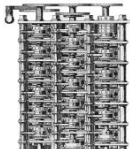
Hens & Rieger (2013)



# Why Do Clients *Actually* Sign OTC Contracts?

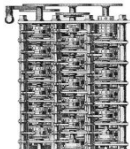
On a scale from the **honest** weak to the **powerful**

- **Desparation**
  - City of Detroit
- **Coercion**
  - Bank loan or loan rollover *requires* accompanying “hedge” derivatives (UK & US SMEs)
- **Trust**
  - Ille Papier v DB German Supreme Court case (2011)
- **Gullability**
  - German Landesbanken (unknown B €)
  - Austrian National Railways (€ 90 M)
  - Milan, Pisa, Sicily, Monte Casino, ... (600 municipalities, over 1000 global deals, c. € 2.5 B lost)
- **Complicity**
  - Italian (1999) (c. € 31 B to 2012) and Greek (2001) (unknown B €) governments for Eurozone entry
  - Monte dei Paschi di Sienna (c. € 8.4 B)
  - Stichting Vestia Group (€ 700 M)



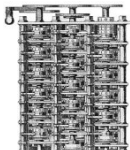
# US Dodd-Frank and Consumer Protection Acts<sup>48</sup>

- Much media attention has been focussed on the **Volker rule** which **partially restores** the **Glass-Steagall Act** of 1933 separating commercial and investment banking (broker-dealers) and **moving OTC derivative trading to cleared exchanges** under the direction of the Commodity Futures Trading Commission
- Specifically **investment banks** must **cease proprietary trading** (i.e. on their own account) and **divest** themselves of **solely-owned hedge and private equity funds**
- The SEC and CFTC have detailed the *implementation* of these acts in July 2013 but much must still be done internationally and it remains to be seen how much teeth they will have
- However clear rules enforcing **duty of care** and **separating advice and trading with clients** specifically for *all governmental entities, pension funds* (Erisa entities) and *foundations* have been overlooked or played down by banks and the media – especially possible **retroactive application**
- In essence this is the motivation behind the **US government's law suits of 18 global derivative issuers over CDO's**



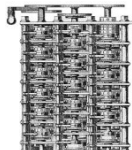
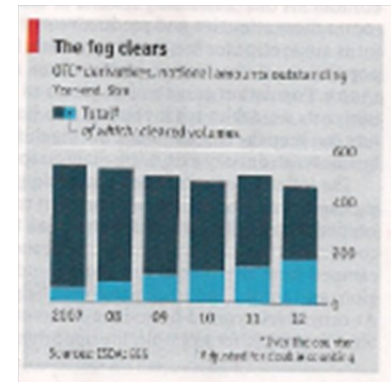
# Basel III

- The Basel Committee recommends imposing a **4.5%** of risk weighted assets **core Tier 1** (equity and retained earnings) capital ratio on banks with a **further 2.5% cushion** which when not met would preclude dividends and executive pay increases
- Although these proposed reforms have been **ratified by the G20** they must be **enacted into law** by the 27 national governments of the Basel agreement **only** from January 2013 **through January 2019**
- The Committee also endorsed a **further 2.5% requirement in boom years** to the basic capital charge and a possible **1.5% systemic risk charge** to global institutions to cushion loss at a downturn although such losses **through the 2007-09 crisis** actually amounted to **7%** globally on average
- Although many leading global banks currently have core Tier 1 capital ratios of over 10% a number of **well known institutions** still **need to raise capital** to meet Basel III requirements including **Barclays, Lloyds and RBS** in the UK, **Société Générale and Crédit Agricole** in France, **Deutsche Bank, Commerz, Hypo Real** and **all the Landesbanken** in Germany and **UniCredit and Banca Intesa IMI** in Italy
- **European bank stress tests** are **widely mistrusted** as their past stress scenarios have **ignored** the **deteriorating sovereign credit of peripheral EU nations** like Greece, Ireland, Portugal and even of Spain and Italy – in Germany such **sovereign bond holdings** were initially **not even reported**



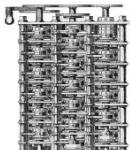
# Client Protection?

- Moving some OTC structured products to cleared exchanges mainly addresses **interbank derivative trading** to which most current regulation is addressed
- **Client** problems could be alleviated by **regulation** to require the *visual display* by banks of the *asymmetric risks* involved in remaining OTC structured products along the lines of the diagrams we have shown for swaps, bonds and FX contracts – unfortunately unlikely for the ongoing Dodd-Frank implementation by the CFTC
- This would result in **fairer products** and encourage the widespread **proper use of derivatives by clients** for hedging various risks
- The concomitant would be a much **smaller margin for banks!**  
Perhaps the BIS recommended **1.5%** rather than the average **10%** ?



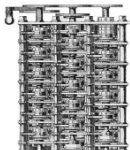
# Barclays Balance Sheet 2012

Assets £ M	Liabilities £ M	
Derivatives 469,146	Derivatives 462,468	
6,679 net		
Loans 425,729	Deposits 385,707	
Other 509,270	Other 579,190	
Cash 86,175	Equity 62,957	4.2 % 24:1
£ 1,490,322 M	£ 1,490,322 M	
£ 1.5 T or <b>61%</b> of <b>UK £2.44 T GDP</b>		



# Systemic Consequences of Derivative Practice<sup>72</sup>

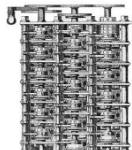
- S&P estimated in 2011 that the top **20 derivatives dealers** with **90% of the OTC market** (those sued by the US government plus UniCredit and Intesa) currently have over **\$500 B each** in these **assets** – a staggering **total** of **\$10 T** and over 3 times the \$3 T global bank *eventual* markdowns estimated at the end of 2008 which are still being realized
- The BIS **total** estimate as of end 2012 was **\$ 21.1 T gross** hedged mark-to-market interbank and corporate plus a further **\$3.6 T net** MTM of un-hedged credit exposure – in large part due to deals of the type we have discussed – at 80% **\$ 2.9 T** or 4% of the \$ 71.7 T 2012 global GDP!
- What would be the **systemic consequences** if a **significant part** of these **cash flows and profits** were to **disappear** due to **regulation/litigation/default**? Exit from serious investment banking is already underway for UBS and under discussion at Credit Suisse and Barclays
- Does Jamie Dimon, CEO of JP Morgan Chase, know something that we don't (even after the 2012 JPM \$ 6.2 B loss and the recent \$ 13 B US government settlement)? On 12<sup>th</sup> September 2011 he was quoted in the *Financial Times* as saying “It could be ‘10 years’ before the (financial) industry emerges from lawsuits brought by investors seeking compensation”





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