



McMaster University



University of Toronto



University of Waterloo

# THE FIELDS INSTITUTE FOR RESEARCH IN MATHEMATICAL SCIENCES

## SEMINAR SERIES ON CONTROL THEORY

**SPEAKER: MIKE ENOS**

The second in a series of four seminars on the topic

### **The Time-Optimal Problem for a Force-Free System of Two Symmetric Rigid Bodies in Three Space**

will be held

**Wednesday, October 23, 1991 at 3:30 p.m.**

in

**Davis Centre 2577  
University of Waterloo**

In this talk, we show that the mechanical system introduced last time is controllable. In particular, we will show that for any choice of endpoints in  $SO(3)^2$ , there is a piecewise-smooth motion of this system consisting of at most three successive motions during each of which the bodies rotate in opposite directions about a fixed axis.

We will prove this result by establishing the following statement for normalized quaternions: Given  $(\lambda_i, \Lambda_i)$ ,  $i = 1, 2$ , there exist  $(\gamma_j, \Gamma_j)$ ,  $1 \leq j \leq 3$ , such that

$$(\gamma_3, \Gamma_3)(\gamma_2, \Gamma_2)(\gamma_1, \Gamma_1) = (\lambda_1, \Lambda_1)$$

and

$$(\gamma_3, \Gamma_3)(\gamma_2, \Gamma_2)(\gamma_1, \Gamma_1) = (\lambda_2, \Lambda_2)$$